



# **SIX SIGMA** M Sc Statistics

Sem III

Paper IV - Industrial Process and Quality  
Control

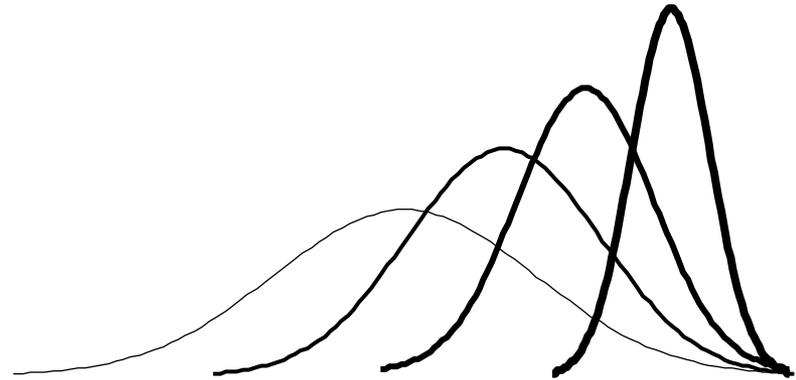
Unit III – SIX SIGMA

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# SIX SIGMA



***A STRATEGY FOR PERFORMANCE  
EXCELLENCE***



# How good is good enough?

## 99.9% is already VERY GOOD

But what could happen at a quality level of 99.9% (i.e., 1000 ppm), in our everyday lives (about  $4.6\sigma$ )?

- **4000 wrong medical prescriptions each year**



- **More than 3000 newborns accidentally falling from the hands of nurses or doctors each year**

- **Two long or short landings at American airports each day**



- **400 letters per hour which never arrive at their destination**



## *How can we get these results*

- **13** wrong drug prescriptions per year
- **10** newborn babies dropped by doctors/nurses per year
- Two short or long landings **per year** in all the airports in the U.S.
- **One** lost article of mail per hour



*The answer is:*

Six Sigma



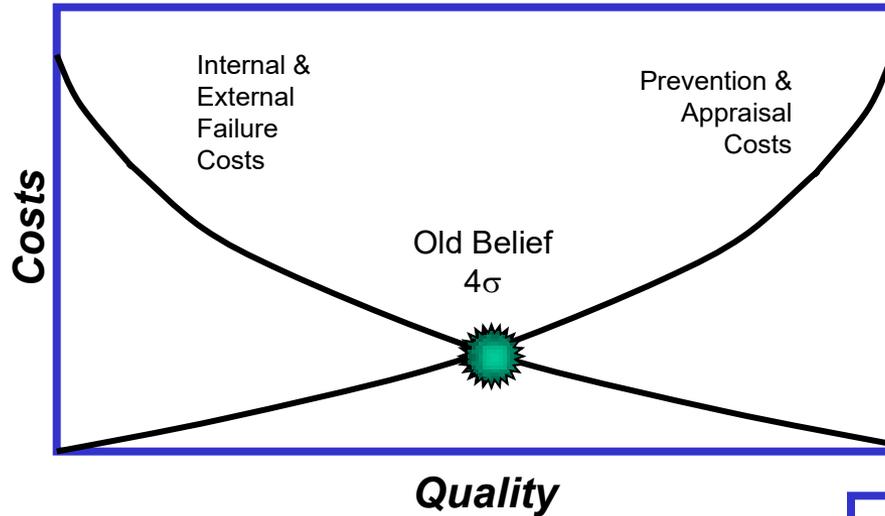
# What is Six Sigma

- A **Vision** and **Philosophical** commitment to our consumers to offer the highest quality, lowest cost products
- A **Metric** that demonstrates quality levels at 99.9997% performance for products and processes
- A **Benchmark** of our product and process capability for comparison to 'best in class'
- A practical application of statistical **Tools** and **Methods** to help us measure, analyze, improve, and control our process





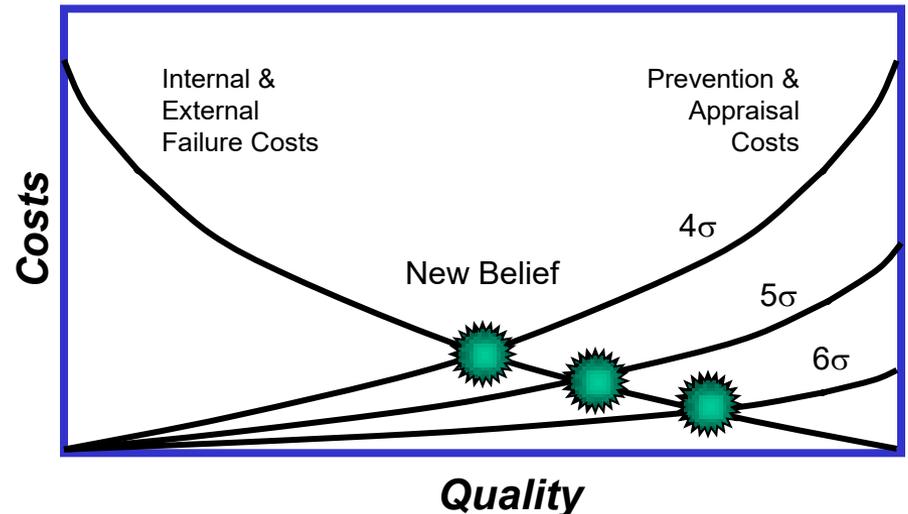
# Six Sigma as a Philosophy



$\sigma$  is a measure of how much variation exists in a process

**Old Belief**

High Quality = High Cost



**New Belief**

High Quality = Low Cost

**Better Processes Reduce Cost**



# 3 Sigma Vs. 6 Sigma

| <i>The 3 sigma Company</i>  | <i>The 6 sigma Company</i>  |
|---|---|
| <ul style="list-style-type: none"><li>• <b><i>Spends 15~25% of sales dollars on cost of failure</i></b></li><li>• <b><i>Relies on inspection to find defects</i></b></li><li>• <b><i>Does not have a disciplined approach to gather and analyze data</i></b></li><li>• <b><i>Benchmarks themselves against their competition</i></b></li><li>• <b><i>Believes 99% is good enough</i></b></li><li>• <b><i>Define CTQs internally</i></b></li></ul> | <ul style="list-style-type: none"><li>• <b><i>Spends 5% of sales dollars on cost of failure</i></b></li><li>• <b><i>Relies on capable process that don't produce defects</i></b></li><li>• <b><i>Use Measure, Analyze, Improve, Control and Measure, Analyze, Design</i></b></li><li>• <b><i>Benchmarks themselves against the best in the world</i></b></li><li>• <b><i>Believes 99% is unacceptable</i></b></li><li>• <b><i>Defines CTQs externally</i></b></li></ul> |



# Focus: The End User

- **Customer: Internal or External**
- **Consumer: The End User**

***the “Voice of the Consumer” (Consumer Cue)  
must be translated into  
the “Voice of the Engineer” (Technical Requirement)***

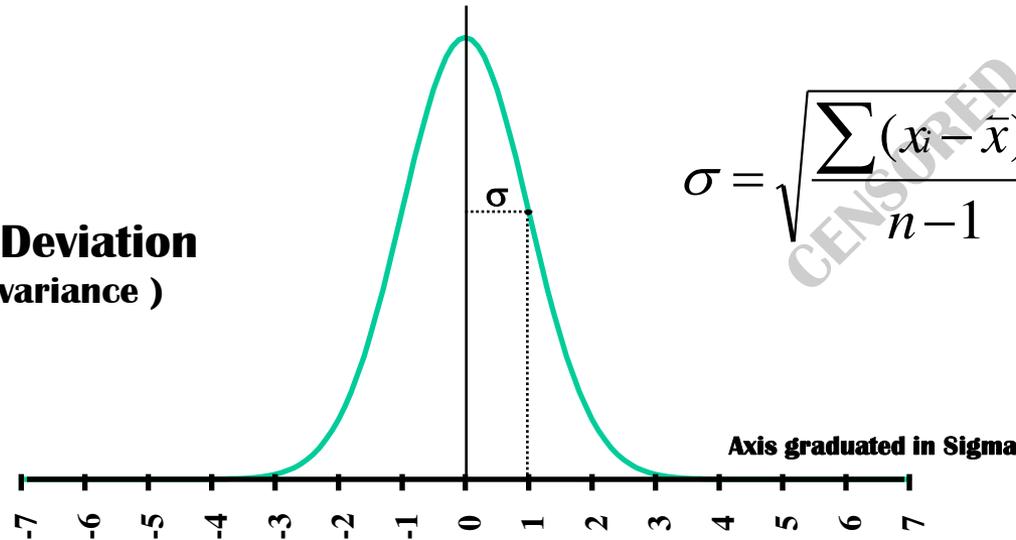




# Six Sigma as a Metric

**Sigma** =  $\sigma$  = **Deviation**  
 ( Square root of variance )

$$\sigma = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} = \text{ASPIRIN}$$



|                        |              |  |
|------------------------|--------------|--|
| between +/- 1 $\sigma$ | 68.27 %      | result: 317300 ppm outside (deviation) |
| between +/- 2 $\sigma$ | 95.45 %      | 45500 ppm                              |
| between +/- 3 $\sigma$ | 99.73 %      | 2700 ppm                               |
| between +/- 4 $\sigma$ | 99.9937 %    | 63 ppm                                 |
| between +/- 5 $\sigma$ | 99.999943 %  | 0.57 ppm                               |
| between +/- 6 $\sigma$ | 99.9999998 % | 0.002 ppm                              |

# 3-sigma Process

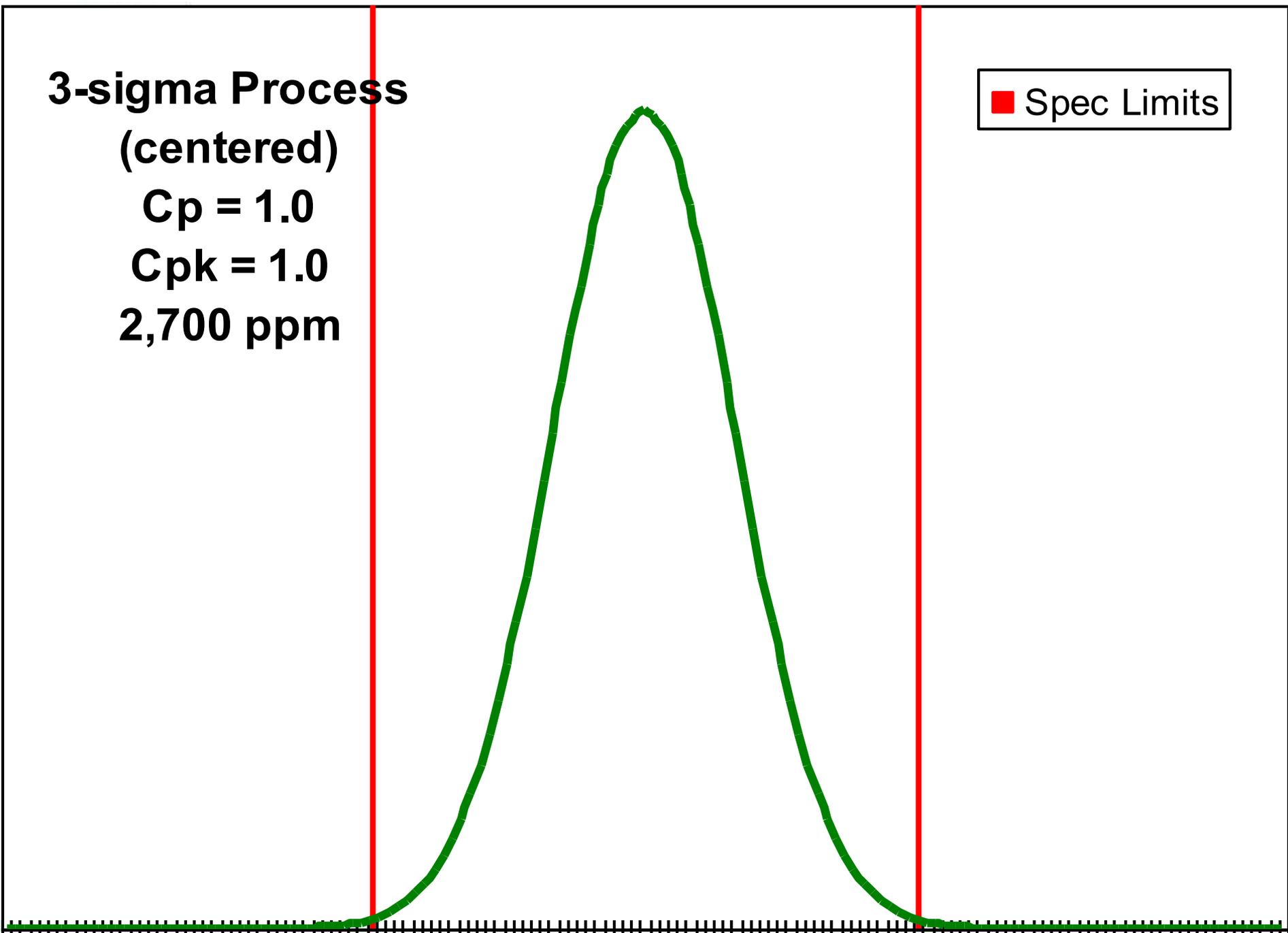
(centered)

$C_p = 1.0$

$C_{pk} = 1.0$

2,700 ppm

■ Spec Limits



**3-sigma Process**  
**(shifted 0.5 std. dev.)**

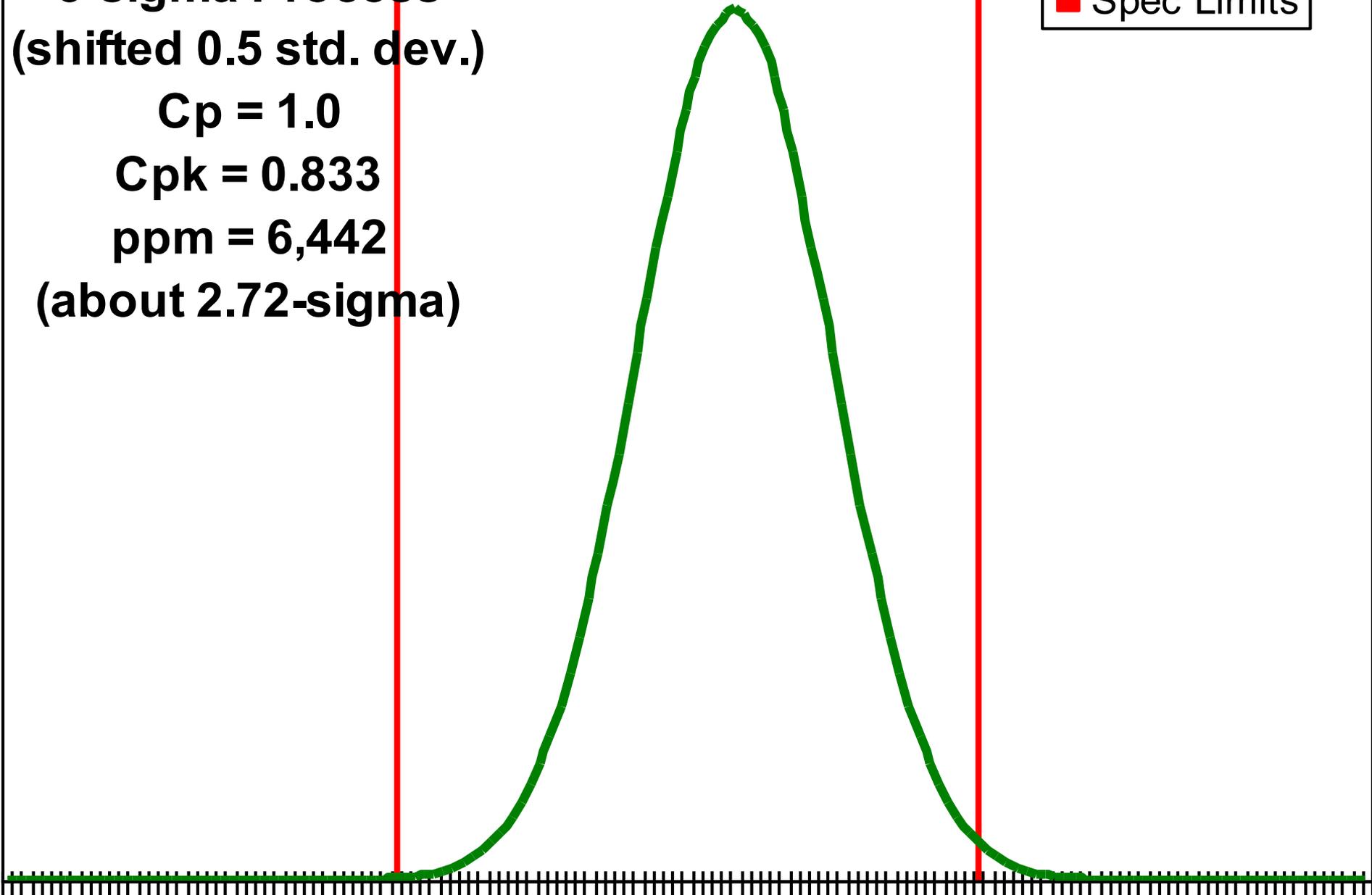
**$C_p = 1.0$**

**$C_{pk} = 0.833$**

**ppm = 6,442**

**(about 2.72-sigma)**

**■ Spec Limits**



**3-sigma Process  
(shifted 1.0 std. dev.)**

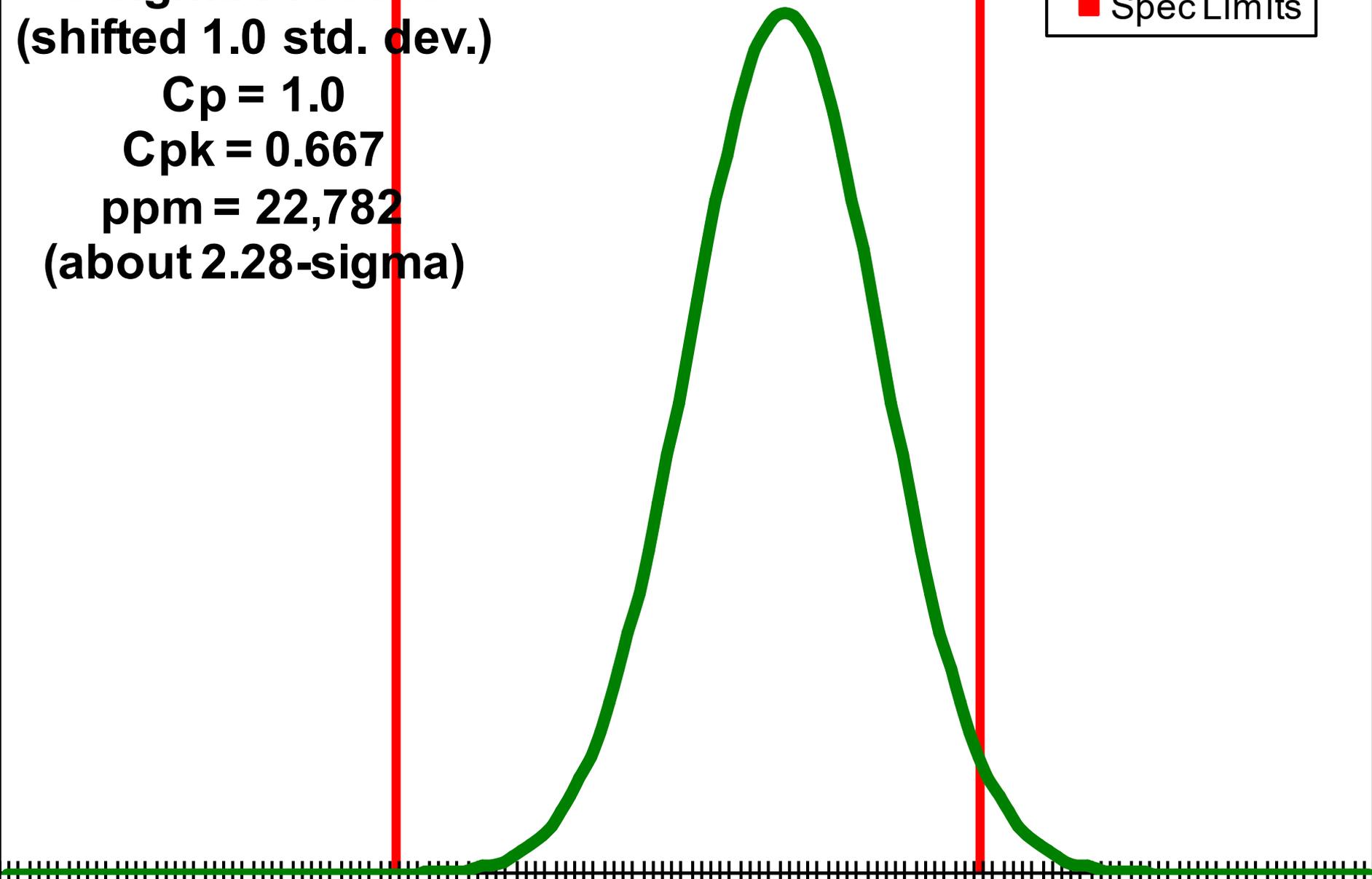
**$C_p = 1.0$**

**$C_{pk} = 0.667$**

**ppm = 22,782**

**(about 2.28-sigma)**

■ Spec Limits



**3-sigma Process  
(shifted 1.5 std. dev.)**

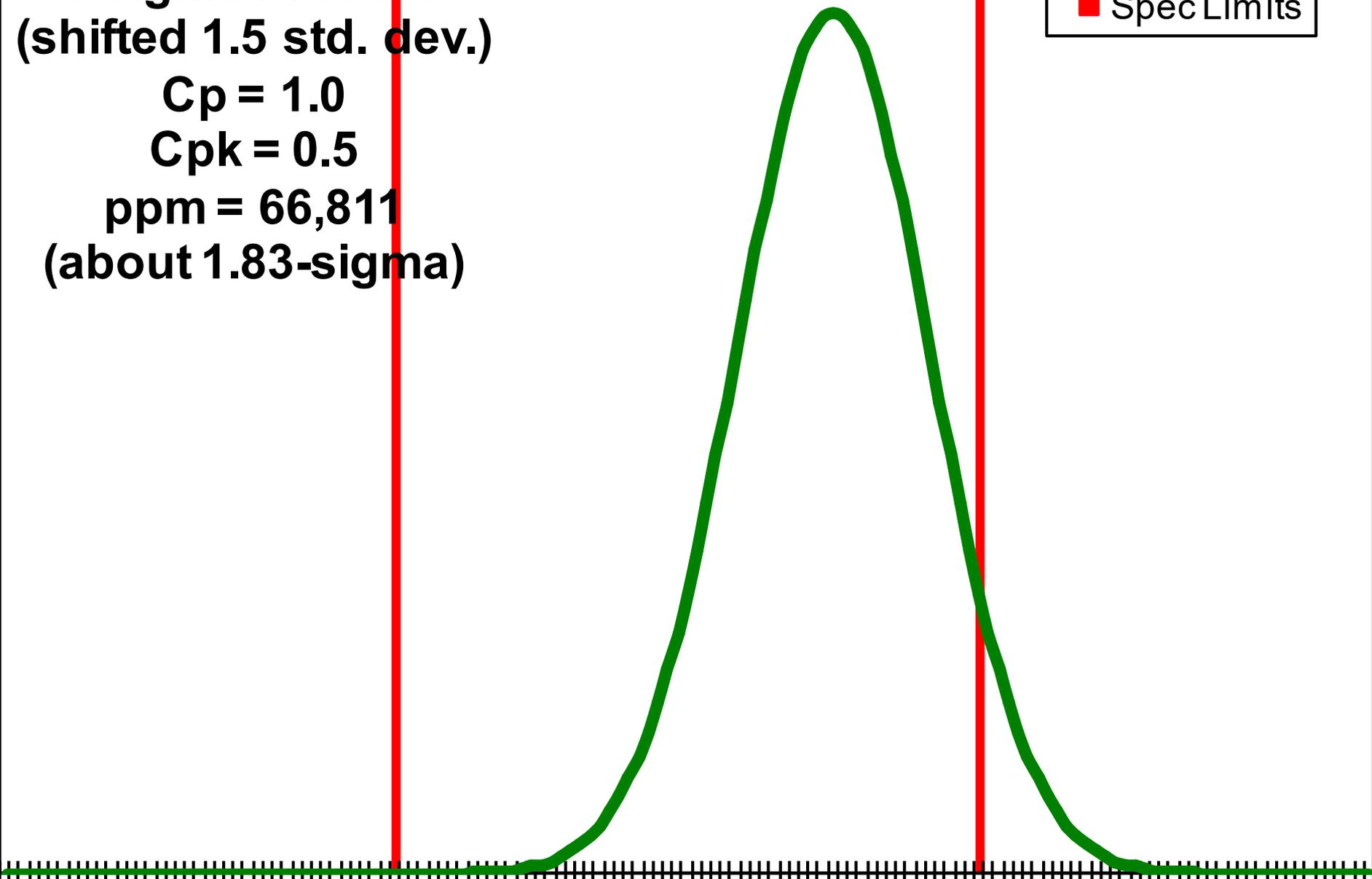
**$C_p = 1.0$**

**$C_{pk} = 0.5$**

**ppm = 66,811**

**(about 1.83-sigma)**

■ Spec Limits



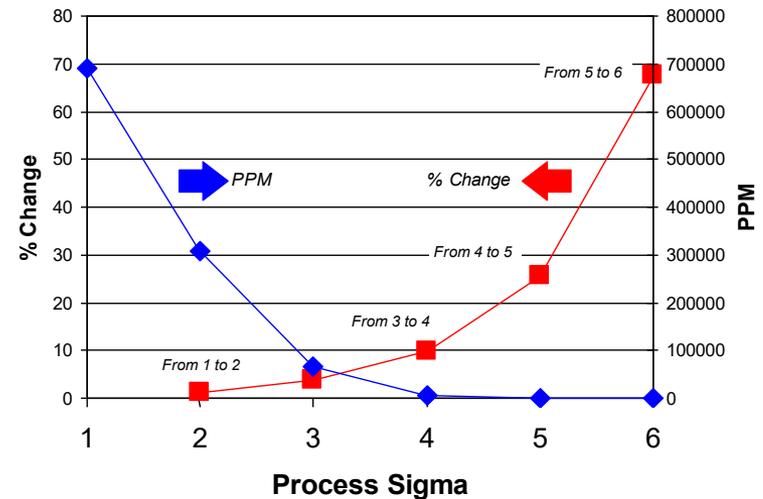


# Non-Linear Decrease

| $\sigma$ | PPM     |
|----------|---------|
| 2        | 308,537 |
| 3        | 66,811  |
| 4        | 6,210   |
| 5        | 233     |
| 6        | 3.4     |

Process Capability      Defects per Million Opportunities

\* Includes 1.5 $\sigma$  shift



**Focusing on  $\sigma$  requires thorough process understanding and breakthrough thinking**



# **Six Sigma as a Tool**

***Process Mapping***

***Tolerance Analysis***

***Structure Tree***

***Components Search***

***Pareto Analysis***

***Hypothesis Testing***

***Gauge R & R***

***Regression***

***Rational Subgrouping***

***DOE***

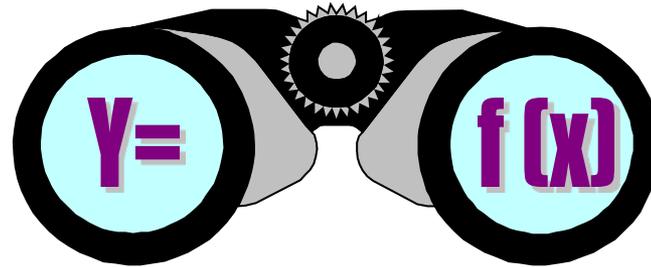
***Baselining***

***SPC***

***Many familiar quality tools applied in a  
*structured methodology****



# Six Sigma as a Method



*To get results, should we focus our behavior on the Y or X*

- 
- Y
  - Dependent
  - Output
  - Effect
  - Symptom
  - Monitor

- X1...Xn
- Independent
- Input-Process
- Cause
- Problem
- Control

# *A Traditional View*



• **Output Variables**

**Manage the outputs.**



# A Non-Traditional View

• **Input Variables**

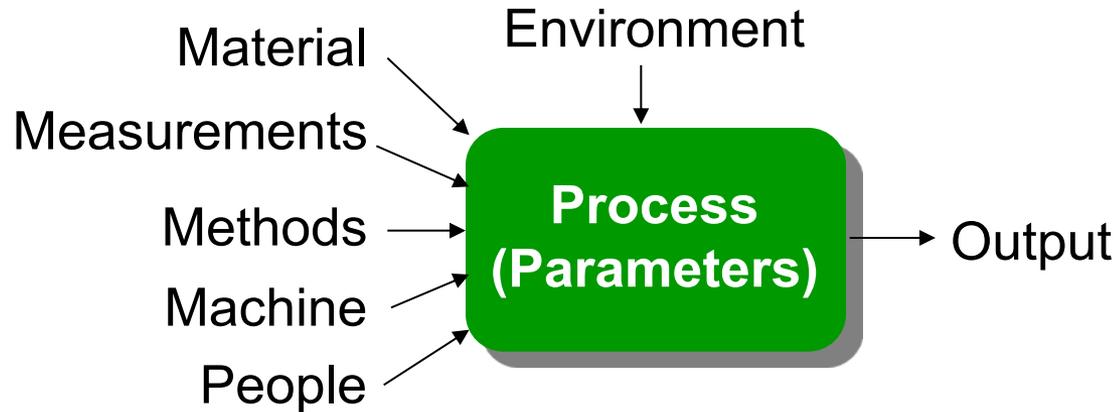


• **Output Variables**

**Manage the inputs; respond to the outputs.**



# Distinguish “Vital Few” from “Trivial Many”



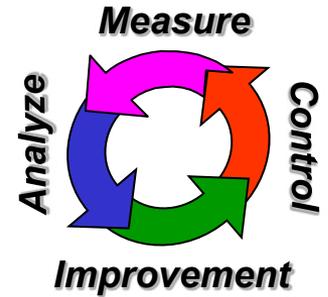
## ***Define the Problem / Defect Statement***

$$Y = f ( X_1^*, X_2, X_3, X_4^*, X_5 \dots X_n )$$

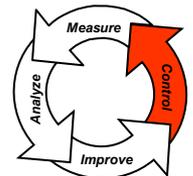
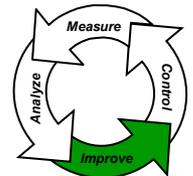
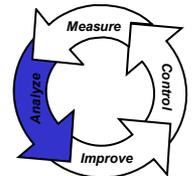
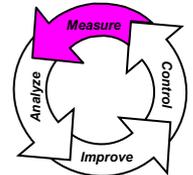
|             |                       |   |                 |
|-------------|-----------------------|---|-----------------|
| <b>Y</b> =  | Dependent Variable    | ➡ | Output, Defect  |
| <b>x</b> =  | Independent Variables | ➡ | Potential Cause |
| <b>x*</b> = | Independent Variable  | ➡ | Critical Cause  |



# Strategy by Phase -



| Phase                                 | Step  | Focus                    |
|---------------------------------------|---|--------------------------|
| <b>Process Characterization</b>       |   |                          |
| <b>Measure</b><br>(What)              | <u>What is the frequency of Defects?</u> <ul style="list-style-type: none"> <li>Define the defect</li> <li>Define performance standards</li> <li>Validate measurement system</li> <li>Establish capability metric</li> </ul>  | Y<br>Y<br>Y<br>Y         |
| <b>Analyze</b><br>(Where, When, Why)  | <u>Where, when and why do Defects occur?</u> <ul style="list-style-type: none"> <li>Identify sources of variation</li> <li>Determine the critical process parameters</li> </ul>   | X<br>Vital X             |
| <b>Process Optimization</b>           |   |                          |
| <b>Improve</b><br>(How)               | <u>How can we improve the process?</u> <ul style="list-style-type: none"> <li>Screen potential causes</li> <li>Discover relationships</li> <li>Establish operating tolerances</li> </ul> <u>Were the improvements effective?</u> <ul style="list-style-type: none"> <li>Re-establish capability metric</li> </ul> | X<br>Vital X<br>Vital X  |
| <b>Control</b><br>(Sustain, Leverage) | <u>How can we maintain the improvements?</u> <ul style="list-style-type: none"> <li>Implement process control mechanisms</li> <li>Leverage project learning's</li> <li>Document &amp; Proceduralize</li> </ul>  | Y, Vital X<br>Y, Vital X |



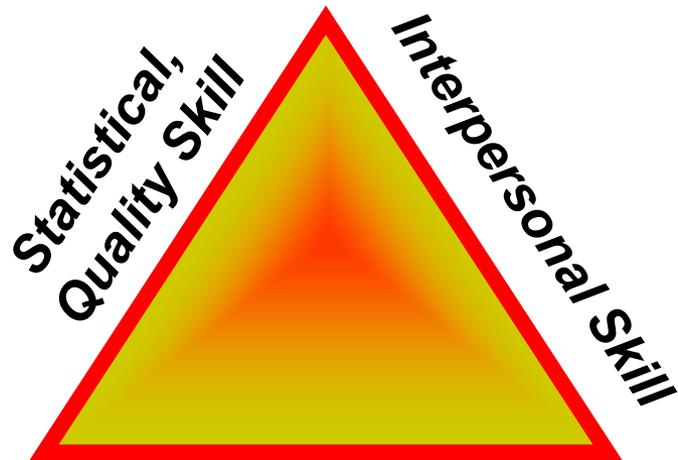


# *Six Sigma Organization*

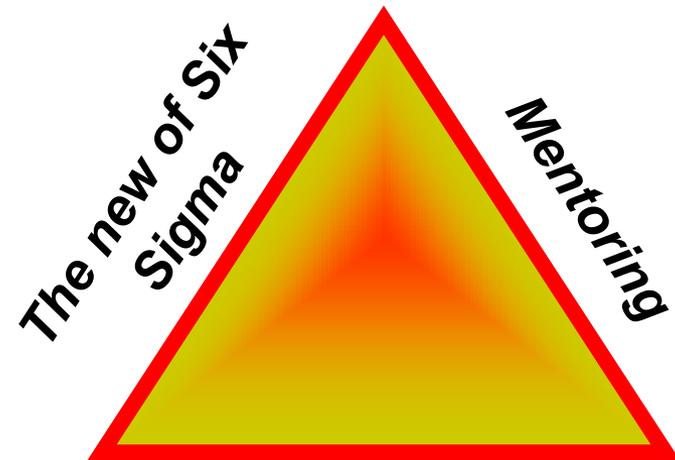




# ***A Black Belt has..., and will...***



***Leadership***



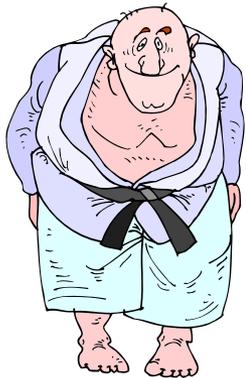
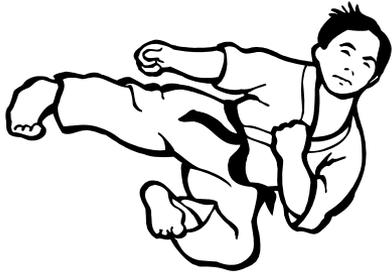
***Driving the Use***



# Black Belt Training



|                          | <b>Task</b>   | <b>Time on Consulting/<br/>Training</b> | <b>Mentoring</b>               | <b>Related Projects</b> |
|--------------------------|---|---|--------------------------------|-------------------------|
| <b>Green Belt</b>        | <i>Utilize Statistical/ Quality technique</i>         | <i>2%~5%</i>                            | <i>Find one new green belt</i> | <i>2 / year</i>         |
| <b>Black Belt</b>        | <i>Lead use of technique and communicate new ones</i> | <i>5%~10%</i>                           | <i>Two green belts</i>         | <i>4 / year</i>         |
| <b>Master Black Belt</b> | <i>Consulting/ Mentoring/ Training</i>                | <i>80~100%</i>                          | <i>Five Black Belts</i>        | <i>10 / year</i>        |

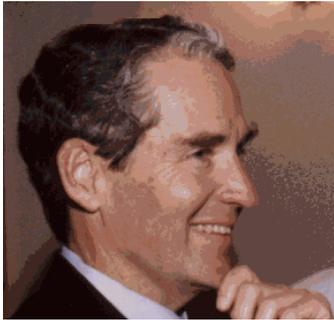




| Core | Statistical Skills  | Core | Six Sigma Quality Skills  | Core | Interpersonal Skills                               |
|------|---|------|---|------|--|
| GBM  | Statistical Software (JMP, Minitab)<br><i>MIN101</i>                                    | GBM  | AIEG OMS  | GBM  | Communication (oral, writ<br><i>AEC722, DDI121</i> |
| GBM  | Numerical and Graphical Techniques<br><i>MIN101, IBM548</i>                             | GBM  | QS 9000<br><i>AEC279</i>  | GBM  | Team Facilitation<br><i>DDI170</i>                 |
| GBM  | Statistical Process Control<br><i>AEC506, AEC661, AEC662, AEC663</i>                    | GBM  | Customer Satisfaction<br><i>SSG100, TCS100</i>                  | GBM  | Coaching and Mentoring<br><i>LDR380, PER119</i>    |
| GBM  | Process Capability<br><i>AEC661, AEC662, SCP201</i>                                     | GBM  | Six Steps to Six Sigma<br><i>SSG100, SSG102CD</i>               | GBM  | Managing Change<br><i>MGT564, MGT124, PDE5.</i>    |
| GBM  | Comparative Tests<br><i>MIN101, SPC201</i>  | GBM  | Concurrent Engineering  | BM   | Leadership<br><i>MGT561, MGT562, DDI18</i>         |
| GBM  | Analysis of Variance (ANOVA)<br><i>ENG998, AEC603</i>                                   | GBM  | TCS<br><i>TCS100</i>  | BM   | Team Building<br><i>MGT560, MGT562, EC727</i>      |
| GBM  | Measurement System Analysis<br><i>AEC663</i>  | GBM  | Systemic Approach to Problem Solving<br><i>QUA392</i>           | M    | Instructional/Teaching<br><i>MOT132</i>            |
| GBM  | Design of Experiments (e.g. Full, Fractional, Taguchi Designs)<br><i>ENG998, QUA389</i> | GBM  | Team Oriented Problem Solving (8D, 7D, 5P)                      | M    | Managing Projects<br><i>AEC471, MGT839</i>         |
| GBM  | Regression (e.g. linear, nonlinear)   | BM   | Quality System Review<br><i>QUA590</i>                          |      |  |
| GBM  | Statistical Process Characterization Strategies and Techniques<br><i>ENG227</i>         | BM   | Team Problem Solving Non-Manufacturing<br><i>CES103</i>         |      |  |
| BM   | Statistical Inference<br><i>MIN101, SPC201</i>  | BM   | Design for Manufacturability<br><i>ENG123, ENG123CD</i>         |      |  |
| BM   | Confidence Intervals<br><i>MIN101, SPC201</i>   | BM   | Financial/Economic Quality Issues                               |      |  |
| BM   | Probability Concepts and Distributions<br><i>SPC201</i>                                 | M    | Quality Function Deployment<br><i>QUA200A, QUA200B, QUA200C</i> |      |  |
| BM   | Response Surface Methods<br><i>QUA393</i>   | M    | Total Quality Management  |      |  |
| BM   | Screening DOE<br><i>QUA391</i>  | M    | Benchmarking<br><i>BMK220</i>                                   |      |  |
| M    | Advanced Problem Solving Strategies and Technologies<br><i>ENG998</i>                   | M    | Product Development Assessment                                  |      |  |
| M    | Acceptance Sampling<br><i>SPC201</i>  |      |   |      |  |
| M    | Sample Size Estimation  |      |   |      |  |
| M    | Robust Design of Processes and Products   |      |   |      |  |
| M    | Survival Analysis / Reliability   |      |   |      |  |



# Corporate Commitment



Motorola is committed to developing these leaders...

We provide these people with extensive training in statistical and interpersonal tools, skilled guidance and management support...

Once their development has achieved a level worthy of recognition, we even have a term for those exceptional individuals :

## ***Six Sigma Black Belts***

Chris Galvin





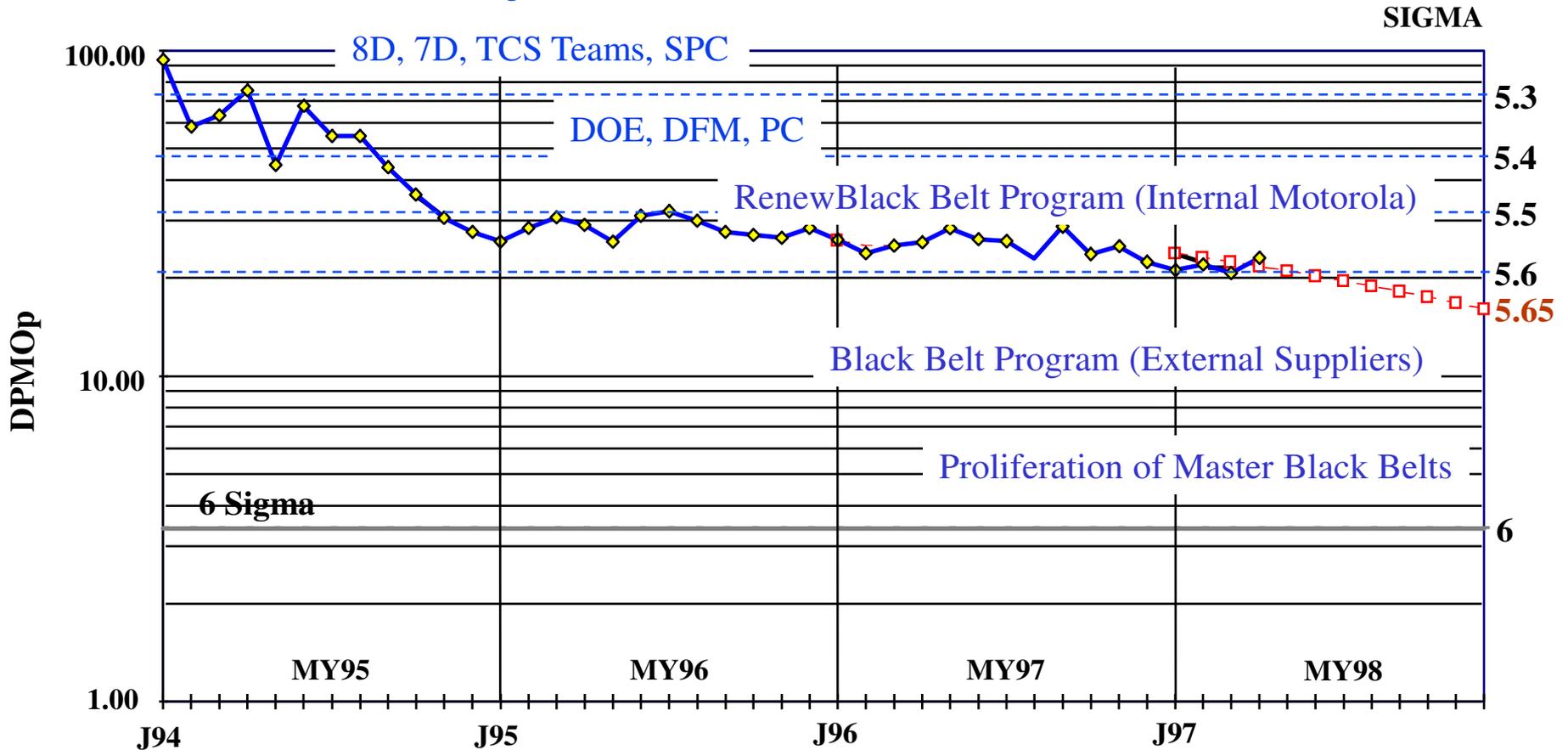
# Corporate Commitment (Cont'd)

- Motto:
  - Quality is our job
  - Customer satisfaction is our duty
  - Customer loyalty is our future



# Barrier Breakthrough Plan

Pareto, Brainstorming, C&E, BvC



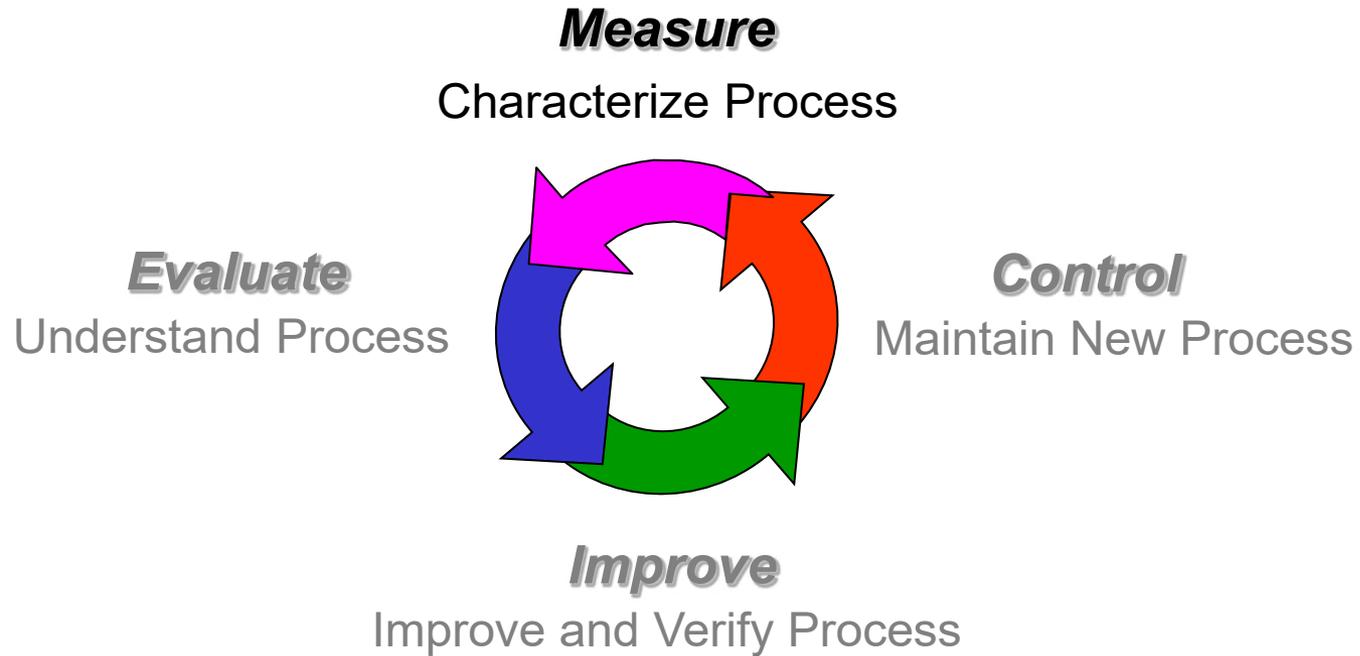


# *Other Companies have Black Belts Program*

- GE has very successfully instituted this program
  - 4,000 trained Black Belts by YE 1997
  - 10,000 trained Black Belts by YE 2000
  - “You haven’t much future at GE unless they are selected to become Black Belts” - Jack Welch
- Kodak has instituted this program
  - CEO and COO driven process
  - Training includes both written and oral exams
  - Minimum requirements: a college education, basic statistics, presentation skills, computer skills
- Other companies include:
  - Allied Signal
  - IBM
  - Navistar
  - Texas Instruments
  - ABB
  - Citibank



# SIX SIGMA





# SIX SIGMA

## Measure Phase

### Define Problem

- Defect Statement
- Project Goals

### Understand Process

- Define Process-  
Process Mapping
- Historical Performance
- Brainstorm Potential Defect Causes

### Collect Data

- Data Types
  - Defectives
  - Defects
  - Continuous
- Measurement Systems Evaluation (MSE)

### Process Performance

- Process Capability
  - Cp/Cpk
  - Run Charts
- Understand Problem (Control or Capability)

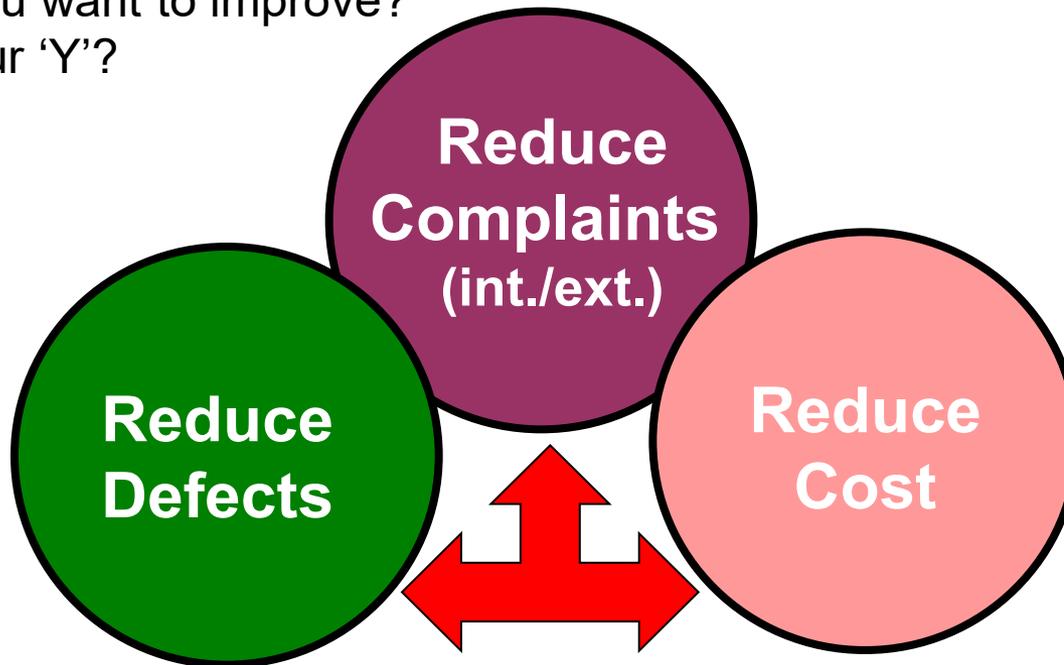
***Understand the Process and Potential Impact***



# SIX SIGMA

## Problem Definition

- ✓ What do you want to improve?
- ✓ What is your 'Y'?



What are the **Goals?**

***Problem Definitions need to be based on quantitative facts supported by analytical data.***



# SIX SIGMA

## **Baselining:**

Quantifying the goodness (or badness!) of the current process, before ANY improvements are made, using sample data. The key to baselining is collecting representative sample data

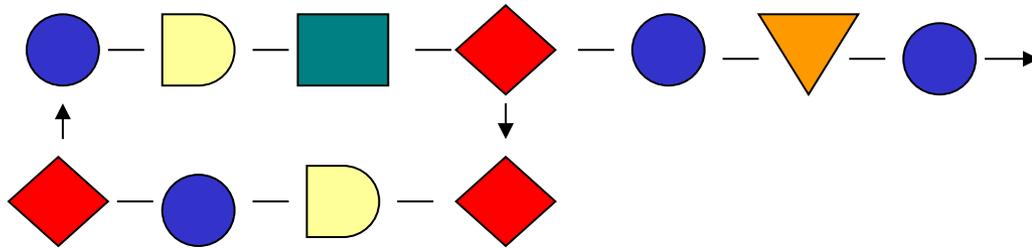
## **Sampling Plan**

- Size of Subgroups
- Number of Subgroups
- Take as many “X” as possible into consideration

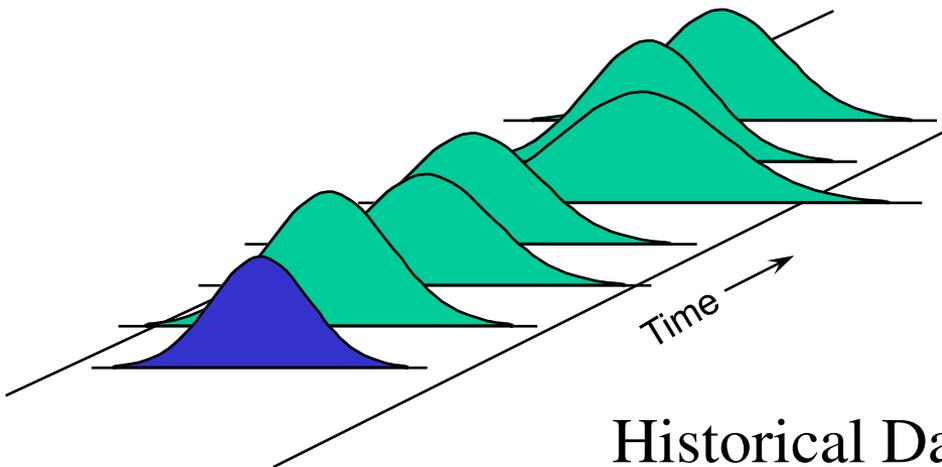


# SIX SIGMA

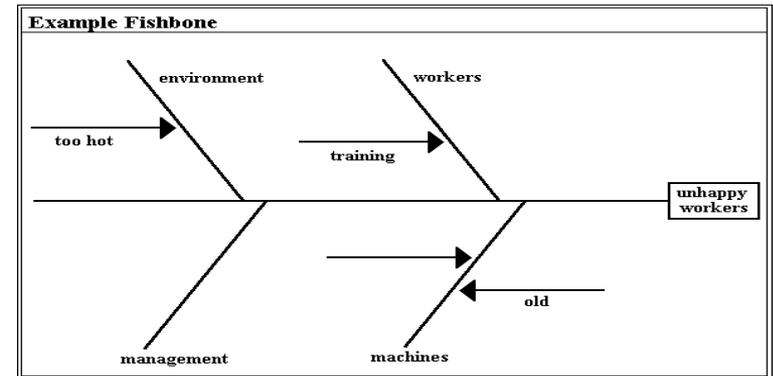
## How do we know our process?



Process Map



Historical Data



Fishbone



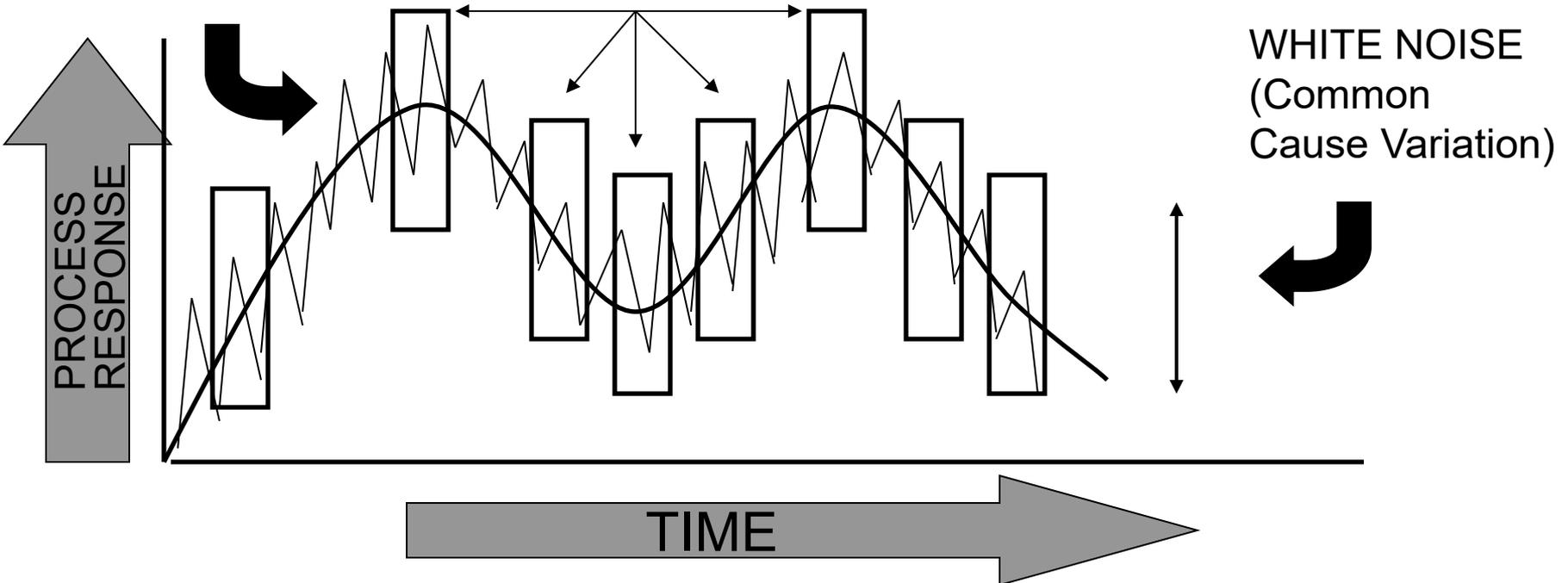
# SIX SIGMA

## RATIONAL SUBGROUPS

Minimize variation within subgroups  
Maximize variation between subgroups

BLACK NOISE  
(Signal)

WHITE NOISE  
(Common  
Cause Variation)



**RATIONAL SUBGROUPING** Allows samples to be taken that include only white noise, within the samples. Black noise occurs between the samples.



# SIX SIGMA

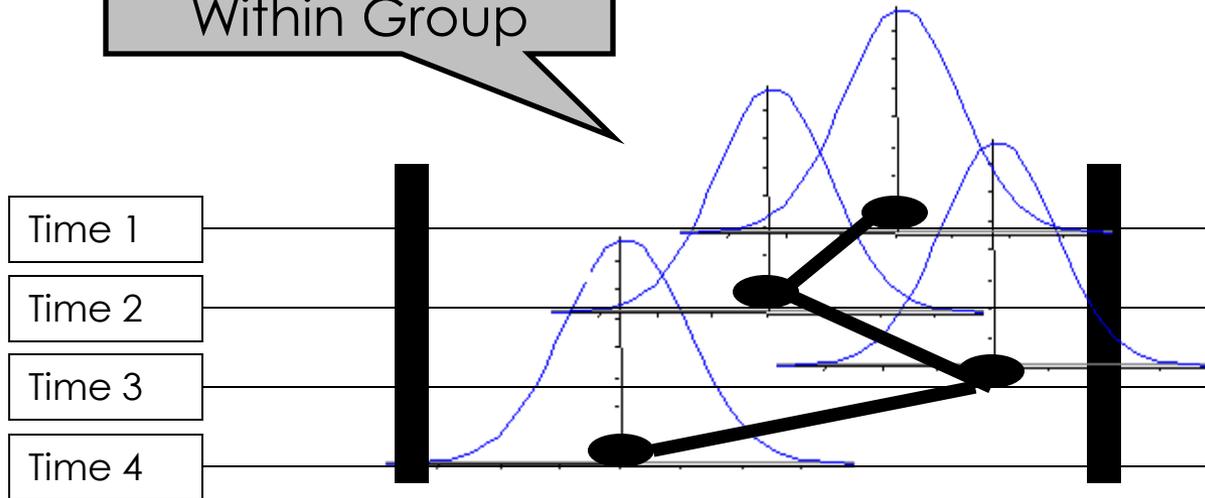
| Sample | Day | Size  | Shift | Operator | Air Pressure |
|--------|-----|-------|-------|----------|--------------|
| 1      | 1   | 0.045 | 1     | 1        | 80           |
| 2      | 1   | 0.046 | 1     | 1        | 80           |
| 3      | 1   | 0.04  | 1     | 1        | 80           |
| 4      | 1   | 0.047 | 1     | 1        | 80           |
| 5      | 1   | -     | 1     | -        | -            |
| 6      | 4   | -     | 2     | -        | -            |
| 7      | 4   | -     | 2     | -        | -            |
| 8      | 4   | -     | 2     | -        | -            |
| 9      | 4   | -     | 2     | -        | -            |
| 10     | 4   | -     | 2     | -        | -            |
| 11     | 3   | -     | 1     | -        | -            |
| 12     | 3   | -     | -     | -        | -            |
| 13     | 3   | -     | -     | -        | -            |
| 14     | -   | -     | -     | -        | -            |



# SIX SIGMA

## Visualizing the Causes

Within Group



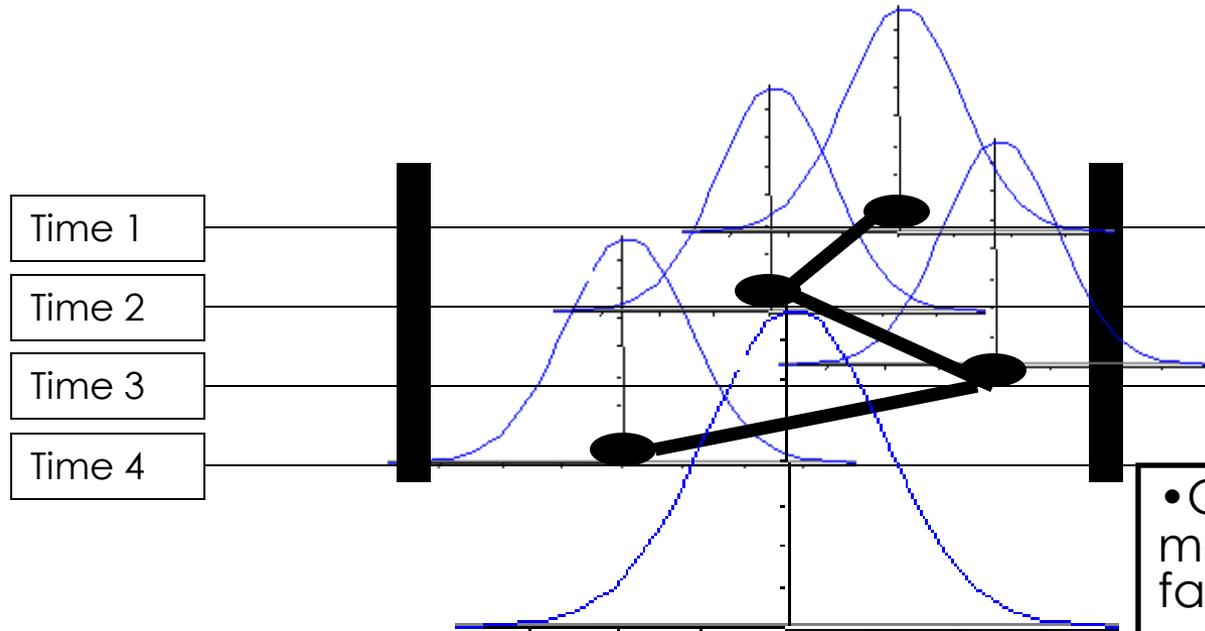
$$\sigma_{st} + \sigma_{shift} = \sigma_{total}$$

- Called  $\sigma$  short term ( $\sigma_{st}$ )
- Our potential – the best we can be
- The s reported by all 6 sigma companies
- The trivial many



# SIX SIGMA

## Visualizing the Causes



$$\sigma_{st} + \sigma_{shift} = \sigma_{total}$$

Between Groups

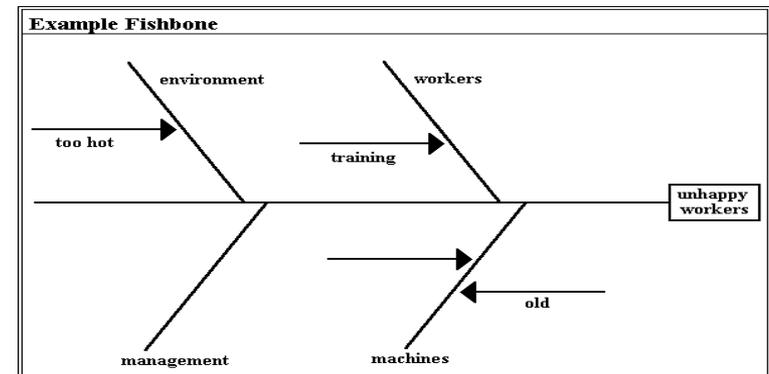
- Called  $\sigma_{shift}$  (truly a measurement in sigmas of how far the mean has shifted)
- Indicates our process control
- The vital few



# SIX SIGMA

## Assignable Cause

- Outside influences
- Black noise
- Potentially controllable
- How the process is actually performing over time



Fishbone



# SIX SIGMA

## Common Cause Variation

- Variation present in every process
- Not controllable
- The best the process can be within the present technology

**Data within subgroups ( $Z_{st}$ ) will contain only Common Cause Variation**



# SIX SIGMA

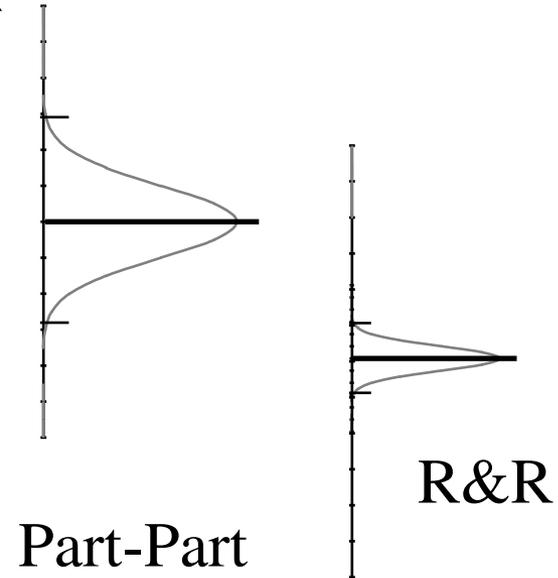
## Gauge R&R

$$\sigma^2_{\text{Total}} = \sigma^2_{\text{Part-Part}} + \sigma^2_{\text{R\&R}}$$

Recommendation:

Resolution  $\leq 10\%$  of tolerance to measure

Gauge R&R  $\leq 20\%$  of tolerance to measure



- **Repeatability (Equipment variation)**

Variation observed with one measurement device when used several times by one operator while measuring the identical characteristic on the same part.

- **Reproducibility (Appraised variation)**

Variation Obtained from different operators using the same device when measuring the identical characteristic on the same part.

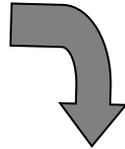
- **Stability or Drift**

Total variation in the measurement obtained with a measurement obtained on the same master or reference value when measuring the same characteristic, over an extending time period.



# SIX SIGMA

Map the Process



Identify the variables - 'x'



Measure the Process

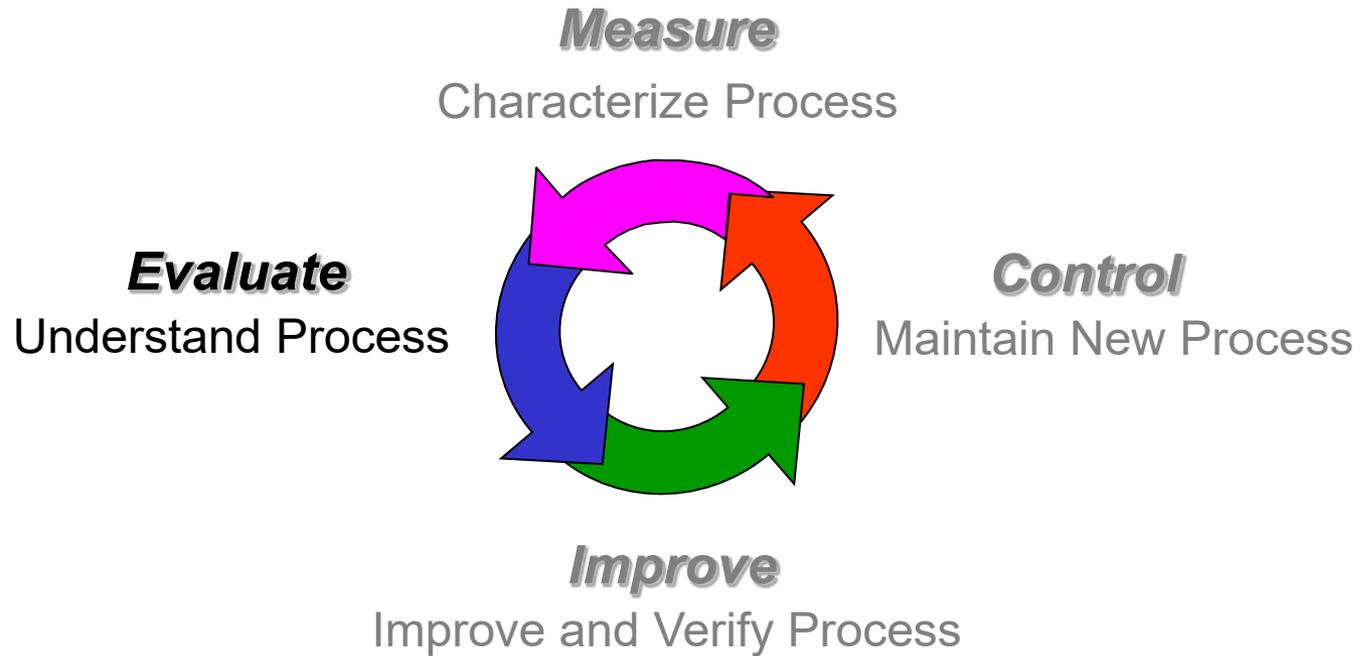


Understand the Problem -  
'Y' = function of variables - 'x'  
 $Y=f(x)$

*To understand where you want to be,  
you need to know how to get there.v*



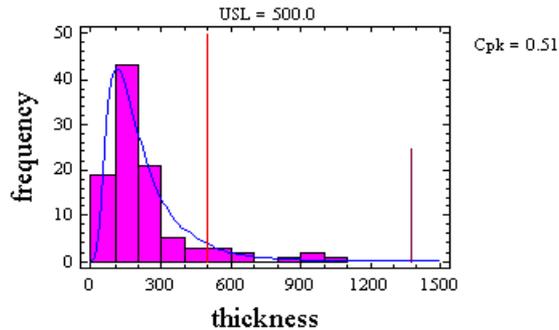
# SIX SIGMA



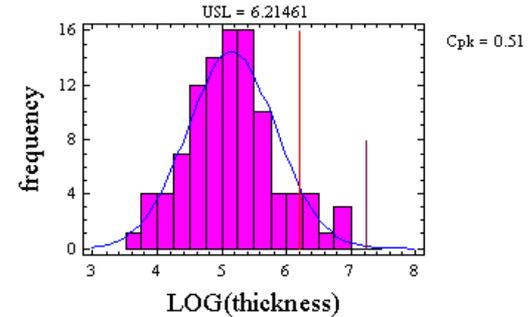


# SIX SIGMA

Process Capability for thickness

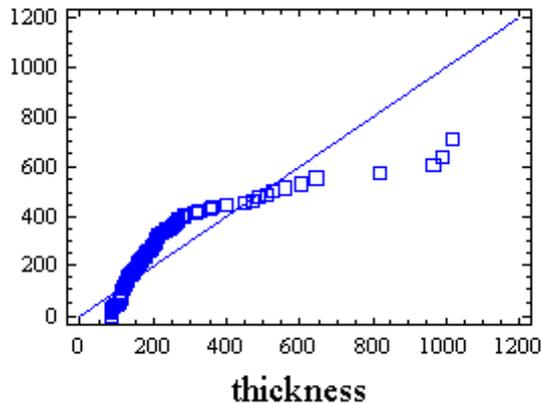


Process Capability for LOG(thickness)

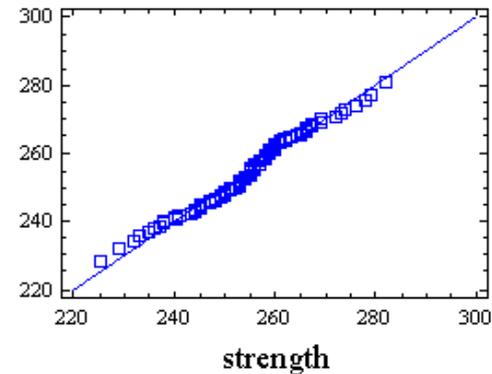


In many cases, the data sample can be transformed so that it is approximately normal. For example, square roots, logarithms, and reciprocals often take a positively skewed distribution and convert it to something close to a bell-shaped curve

Probability Plot



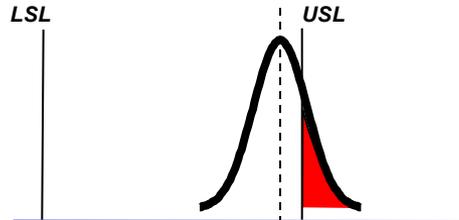
Probability Plot



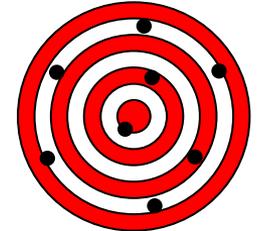
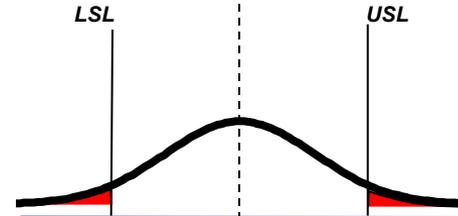


# SIX SIGMA

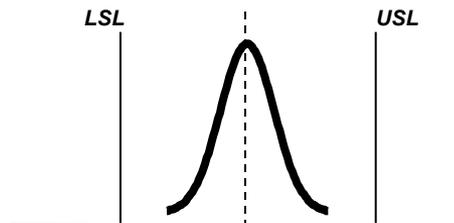
What do we Need?



*Off-Target, Low Variation  
High Potential Defects  
Good Cp but Bad Cpk*



*On Target  
High Variation  
High Potential Defects  
No so good Cp and Cpk*



*On-Target, Low Variation  
Low Potential Defects  
Good Cp and Cpk*

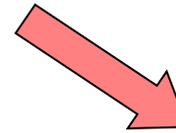
- Variation reduction and process centering create processes with less potential for defects.
- The concept of defect reduction applies to **ALL** processes (not just manufacturing)



# SIX SIGMA

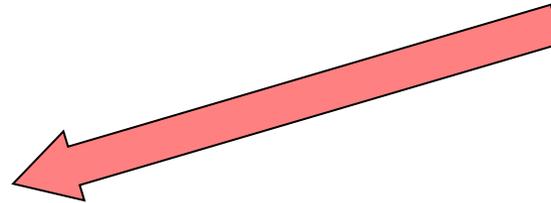
## Eliminate “Trivial Many”

- Qualitative Evaluation
- Technical Expertise
- Graphical Methods
- Screening Design of Experiments



## Identify “Vital Few”

- Pareto Analysis
- Hypothesis Testing
- Regression
- Design of Experiments



## Quantify Opportunity

- % Reduction in Variation
- Cost/ Benefit

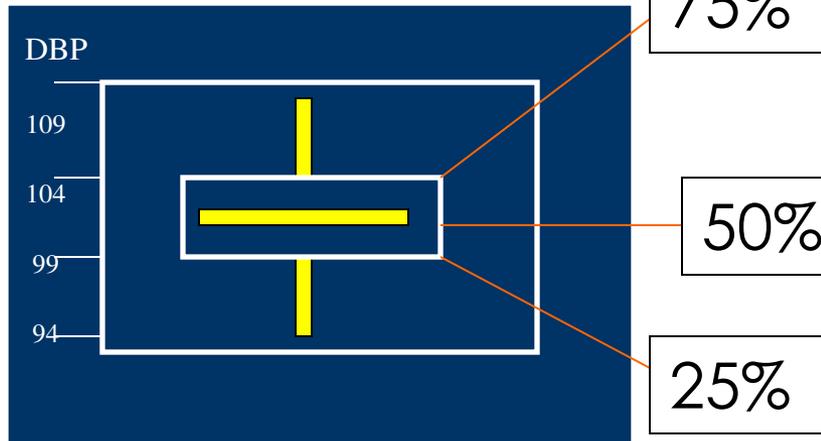
**Our Goal:  
Identify the Key Factors (x's)**



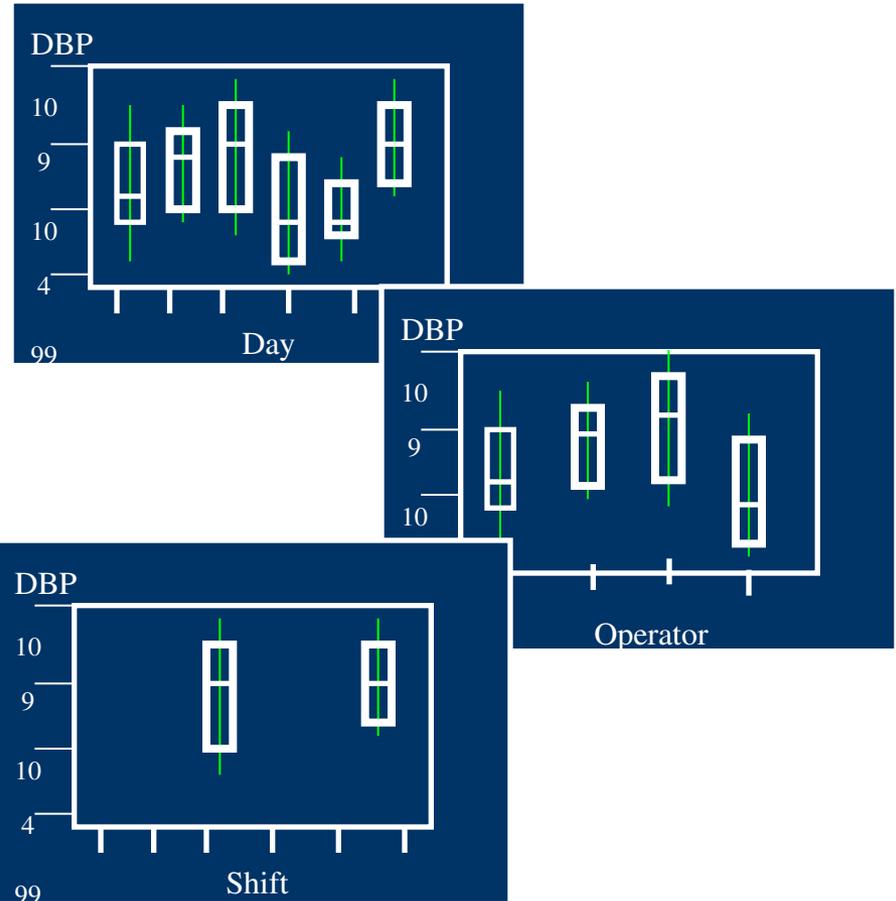
# SIX SIGMA

Graph>Box plot

Without X values



Graph>Box plot



Box plots help to see the data distribution

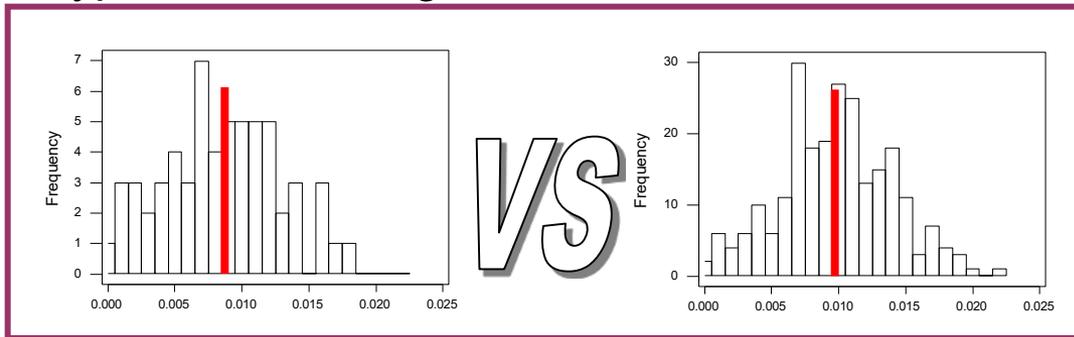


# SIX SIGMA

## Statistical Analysis

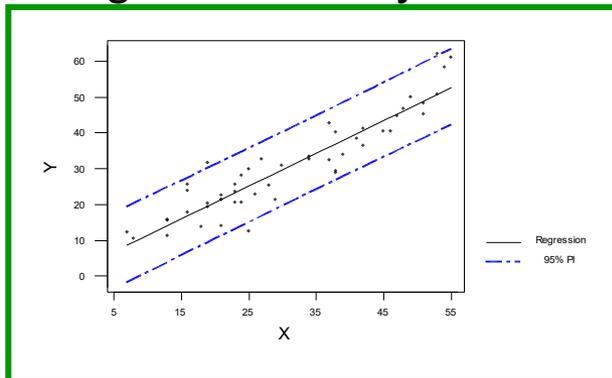
Apply statistics to validate actions & improvements

### Hypothesis Testing



*Compare  
Sample Means  
& Variances*

### Regression Analysis

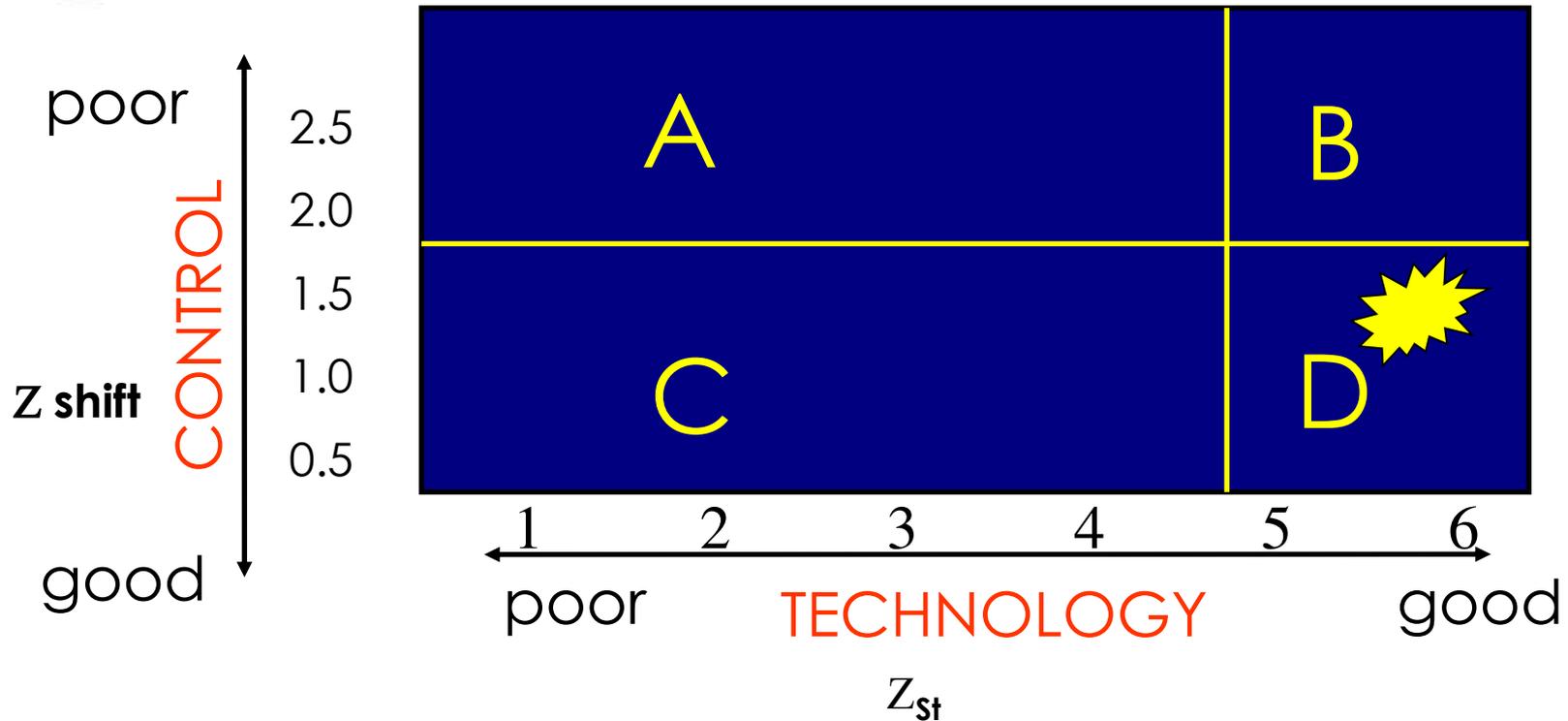


*Identify  
Relationships  
Establish  
Limits*

- Is the factor really important?
- Do we understand the impact for the factor?
- Has our improvement made an impact
- What is the true impact?



# SIX SIGMA



A- Poor Control, Poor Process

B- Must control the Process better, Technology is fine

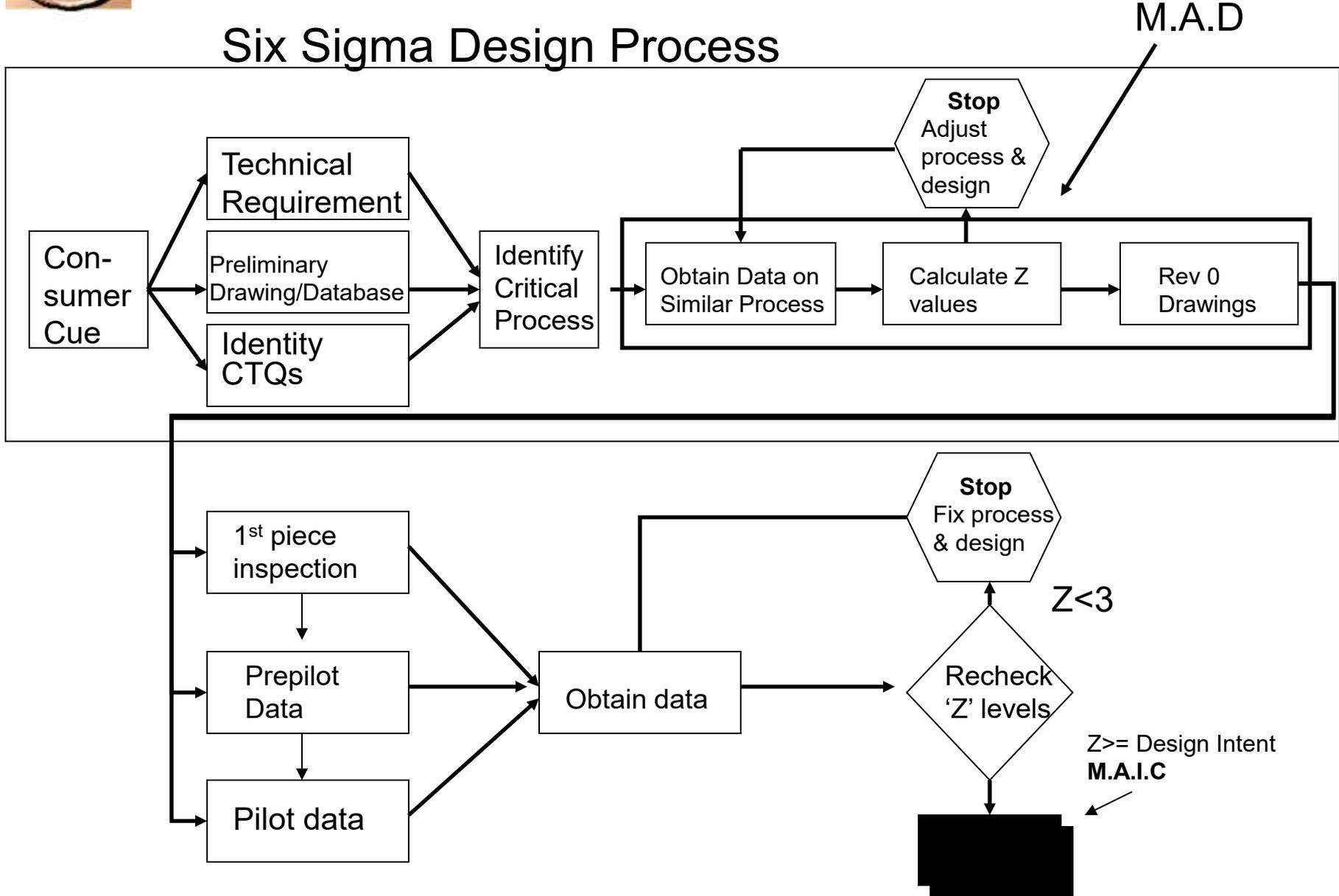
C- Process control is good, bad Process or technology

D- World Class



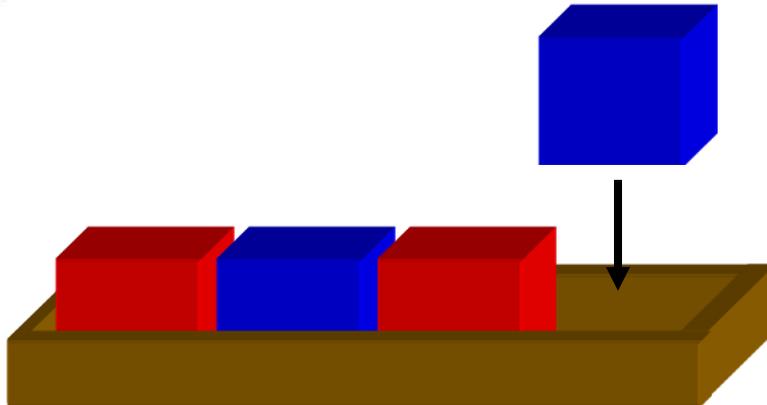
# SIX SIGMA

## Six Sigma Design Process





# SIX SIGMA



| Reliability (Level)                | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
|------------------------------------|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|
| Time to install                    |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Time to repair                     |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Time to service                    |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Service Reliability                |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Response time to service loss      |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Voltage                            |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Power                              |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Time to supply electrical Power    |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Backup power capacity (time)       |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Service Sensitivity                |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Power Lossing                      |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Time Between maintenance           |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Time between equipment replacement |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Failure Index Rating               |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Cost of installation               |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Cost of maintenance                |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Cost of installation               |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Level of Maintenance needed        |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Customer Support Rating            |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Dependence on weather conditions   |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| EC/Compliance                      |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| Hours of training req'd            |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |

| Customer Requirements                        | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 |
|--|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|
| 1 Fast Response                              |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 2 Long time of life span                     |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 3 Low environmental cost                     |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 4 Safe to operate                            |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 5 Mean power requirements                    |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 6 Low investment cost                        |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 7 Excessive small floor space                |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 8 Easy to upgrade                            |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 9 Low operating cost                         |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 10 Low time to implement                     |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 11 Cheap to maintain                         |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 12 Low response to cycle time                |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 13 Easy life cycle of the external component |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 14 Hard to upgrade                           |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 15 Cheap to install                          |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |
| 16 Easy Existing process technology          |   |   |   |   |   |   |   |   |   |    |    |    |    |    |    |    |

**QFD, FMEA, RTY**

- #1 Define the customer Cue and technical requirement we need to satisfy

**Consumer Cue:** Blocks Cannot rattle and must not interfere with box

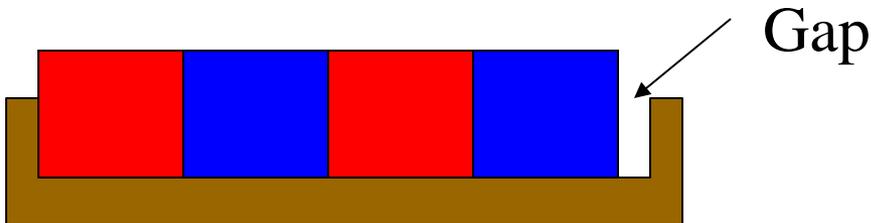
**Technical Requirement:** There must be a positive Gap



# SIX SIGMA



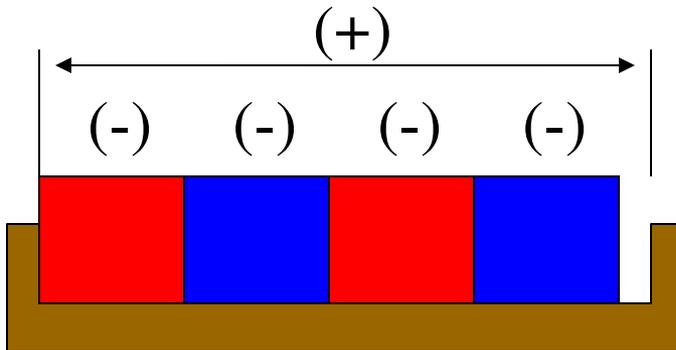
- #2 Define the target dimensions (New designs) or process mean (existing design) for all mating Parts



Gap Must Be  $T=.011$ ,  $LSL=.001$  and  $USL = .021$



# SIX SIGMA



## Gap Requirements

$$\mu_T = .010$$

$$USL = .020$$

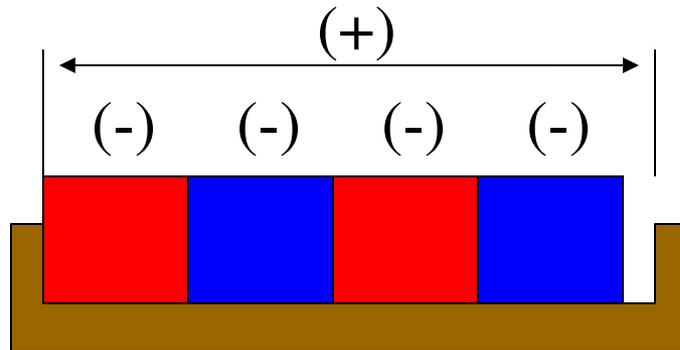
$$LSL = .001$$

## Step #3

- Gather process capability data.
- Use actual or similar part data to calculate SS of largest contributors.
- May use expert data for minimal contributors
- Do not calculate s from current tolerances



# SIX SIGMA



From process:

|      | Average | $\sigma_{st}$ |
|------|---------|---------------|
| Cube | 1.250   | .001          |
| Box  | 5.080   | .001          |

$$\mu_{\text{gap}} = \mu_{\text{box}} - \mu_{\text{cube1}} - \mu_{\text{cube2}} - \mu_{\text{cube3}} - \mu_{\text{cube4}}$$

$$Z_{\text{shift}} = 1.6$$

$$\sigma_{\text{gap}} = \sqrt{\sigma_{\text{box}}^2 + \sigma_{\text{cube1}}^2 + \sigma_{\text{cube2}}^2 + \sigma_{\text{cube3}}^2 + \sigma_{\text{cube4}}^2}$$

Short Term

$$\mu_{\text{gap}} = 5.080 - 1.250 - 1.250 - 1.250 - 1.250 = .016$$

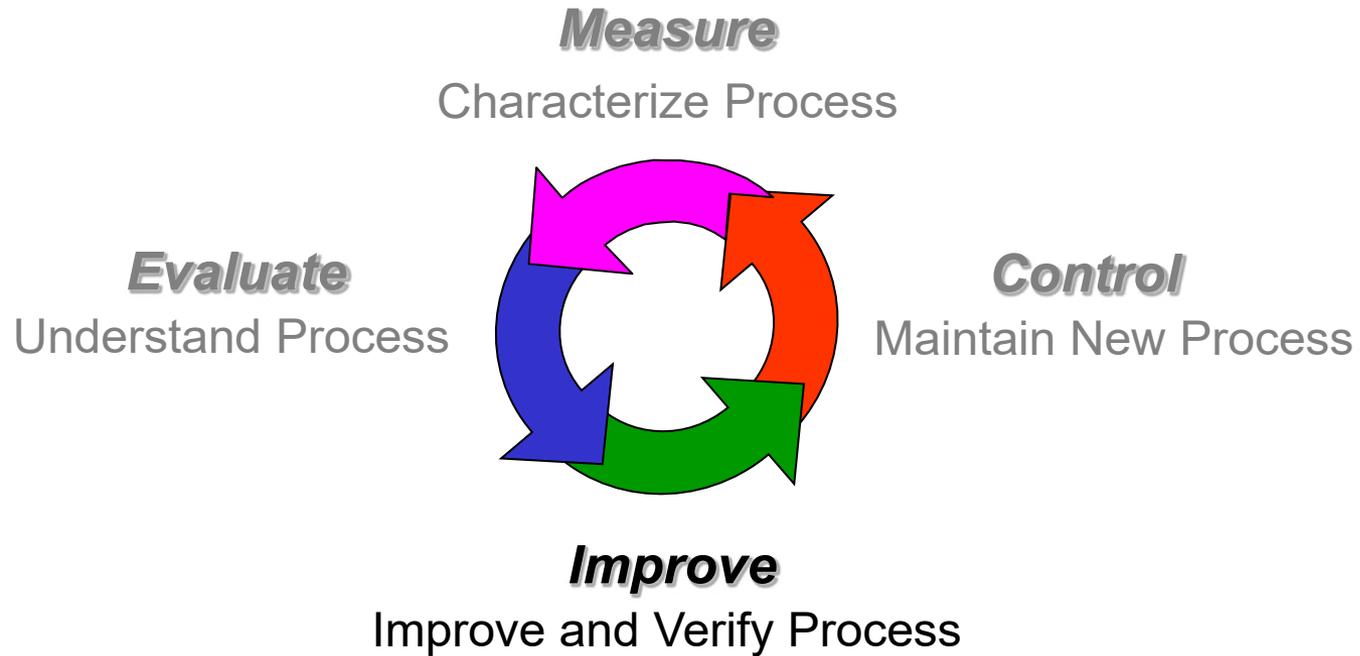
$$\sigma_{\text{gap}} = \sqrt{(.001)^2 + (.001)^2 + (.001)^2 + (.001)^2 + (.001)^2} = .00224$$

Long Term

$$\sigma_{\text{gap}} = \sqrt{(.0015)^2 + (.0015)^2 + (.0015)^2 + (.0015)^2 + (.0015)^2} = .00335$$



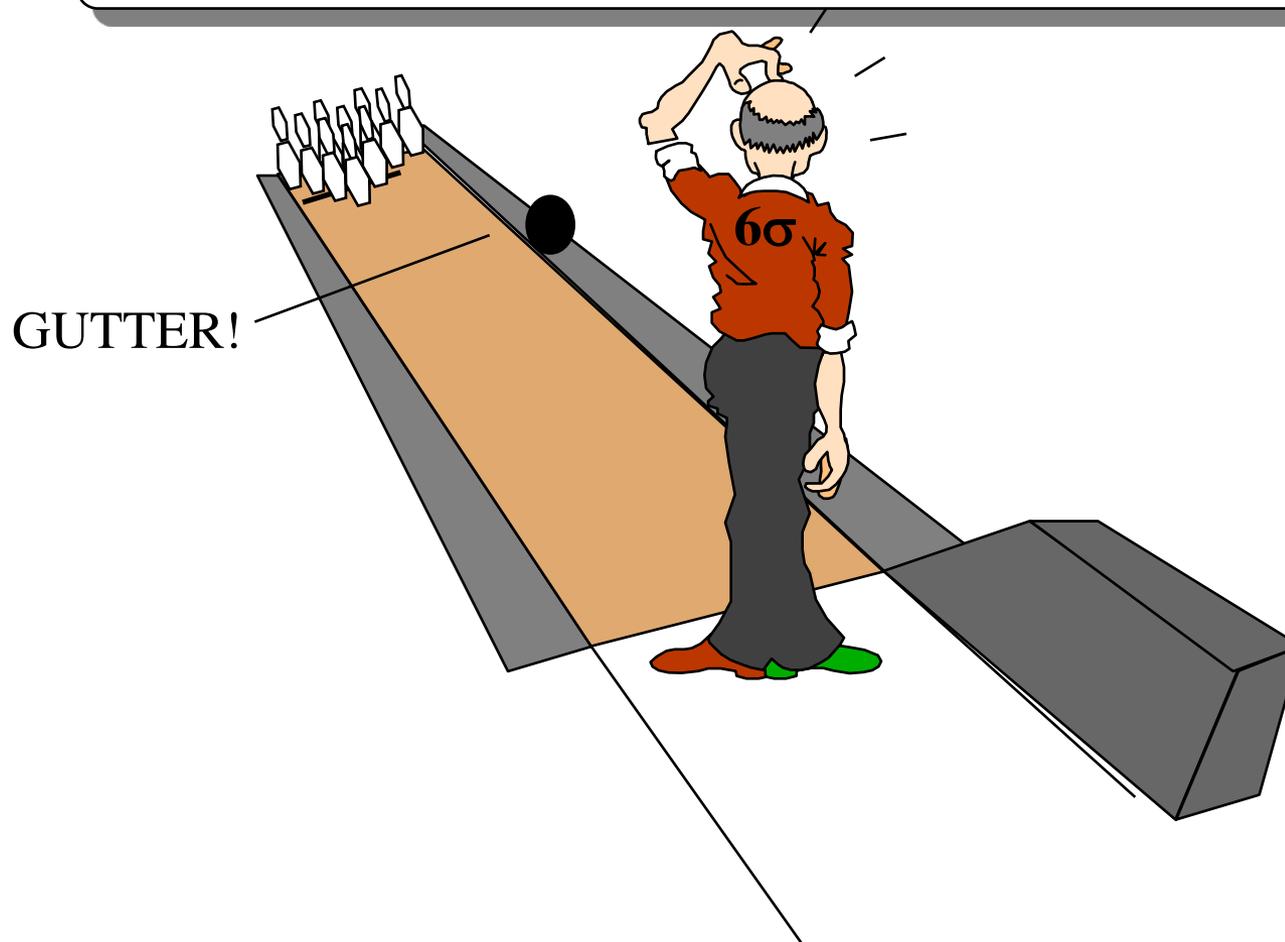
# SIX SIGMA





# SIX SIGMA

What Do I need to do to improve my Game?





# SIX SIGMA

## Design of Experiments (DOE)

- To estimate the effects of independent Variables on Responses.



- Terminology
  - Factor – An independent variable
  - Level – A value for the factor.
  - Response - Outcome



# SIX SIGMA

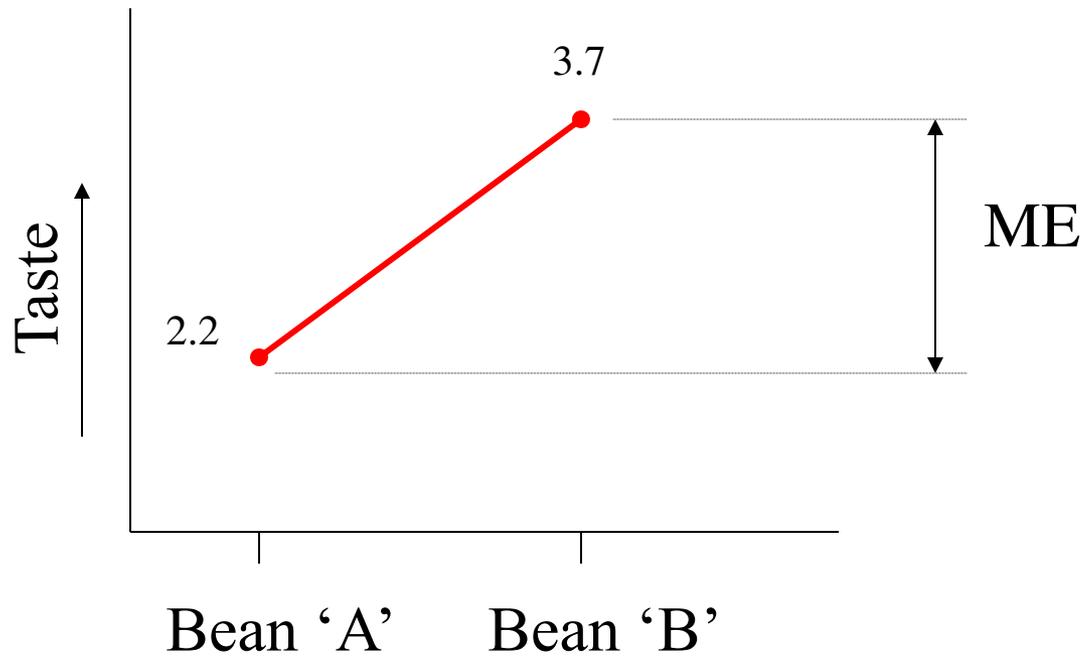
## THE COFFEE EXAMPLE

| Factor        | Level         |                   |
|---------------|---------------|-------------------|
|               | Low           | High              |
| Coffee Brand  | Maxwell House | Chock Full o Nuts |
| Water         | Spring        | Tap               |
| Coffee Amount | 1             | 2                 |



# SIX SIGMA

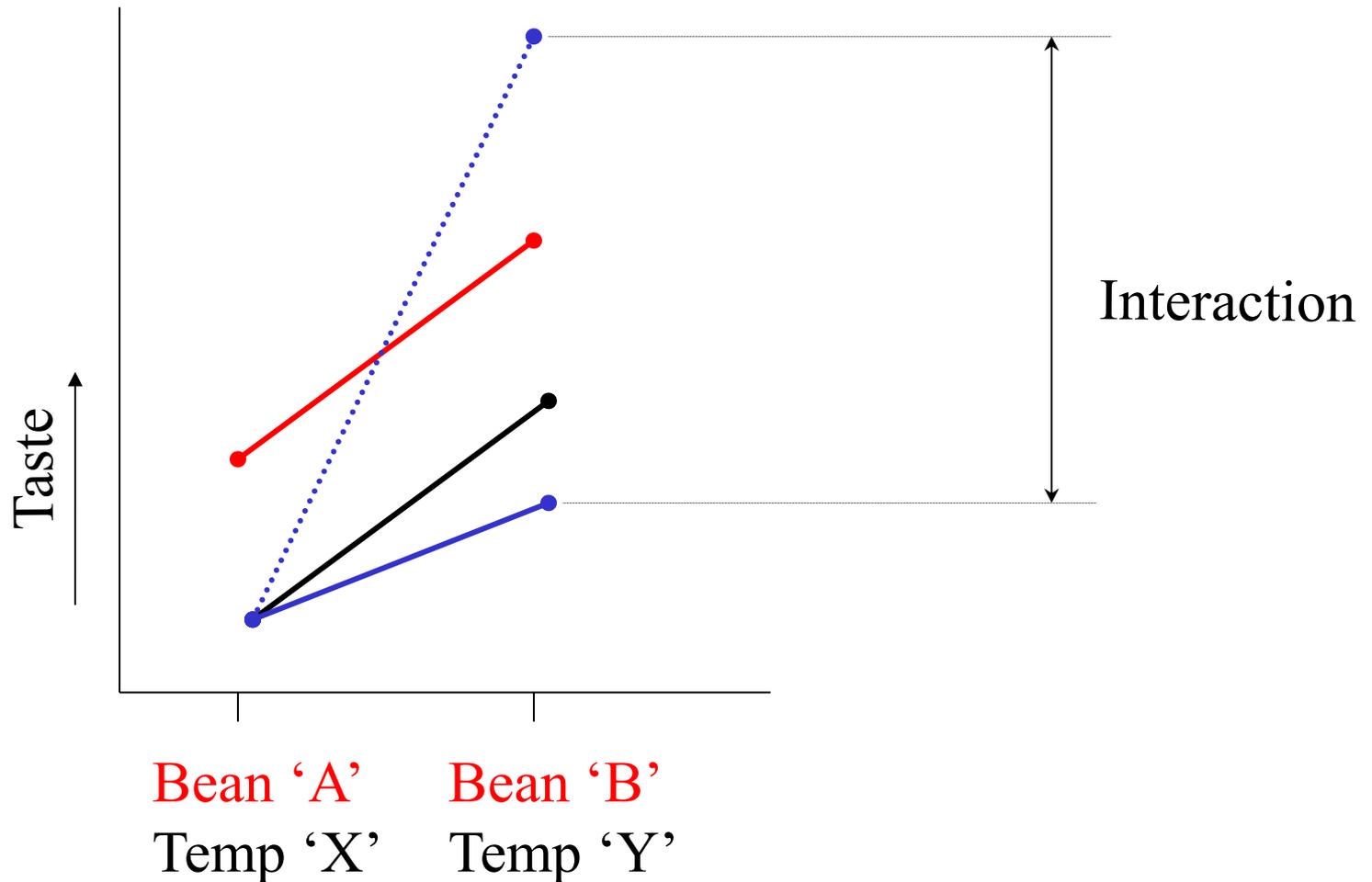
**Main Effects:** Effect of each individual factor on response





# SIX SIGMA

## Concept of Interaction

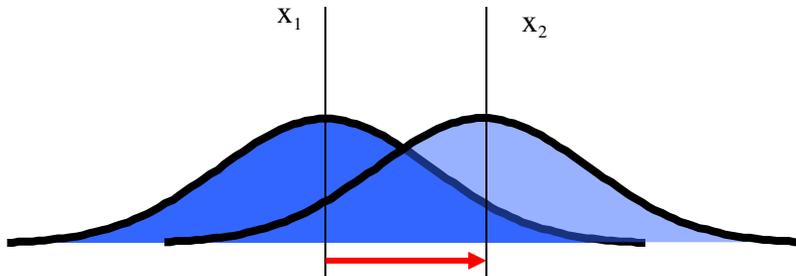




# SIX SIGMA

## Why use DoE ?

- Shift the average of a process.



- Reduce the variation.



- Shift average and reduce variation



# SIX SIGMA

## DoE techniques

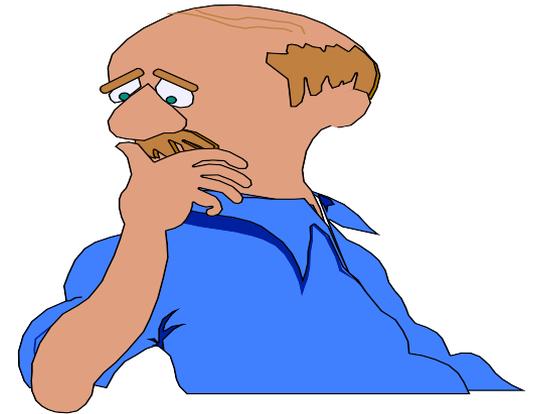
- Full Factorial.
  - $2^4 = 16$  trials
  - 2 is number of levels
  - 4 is number of factors
- All combinations are tested.
- Fractional factorial can reduce number of trials from 16 to 8.



# SIX SIGMA

## DoE techniques....contd.

- Fractional Factorial
- Taguchi techniques
- Response Surface Methodologies
- Half fraction





# SIX SIGMA

## Mini Case - NISSAN MOTOR COMPANY



| Factor                           | Level |         |
|----------------------------------|-------|---------|
|                                  | High  | Low     |
| Adhesion Area (cm <sup>2</sup> ) | 15    | 20      |
| Type of Glue                     | Acryl | Urethan |
| Thickness of Foam Styrene        | Thick | Thin    |
| Thickness of Logo                | Thick | Thin    |
| Amount of pressure               | Short | Long    |
| Pressure application time        | Small | Big     |
| Primer applied                   | Yes   | No      |



# SIX SIGMA

## Design Array

A - Adhesion Area (cm<sup>2</sup>)

B - Type of Glue

C - Thickness of Foam Styrene

D - Thickness of Logo

| No | A | B | C | D | Gluing Str |
|----|---|---|---|---|------------|
| 1  | + | + | + | - | 9.8        |
| 2  | + | + | - | - | 8.9        |
| 3  | + | - | + | + | 9.2        |
| 4  | + | - | - | + | 8.9        |
| 5  | - | + | + | - | 12.3       |
| 6  | - | + | - | - | 13         |
| 7  | - | - | + | + | 13.9       |
| 8  | - | - | - | + | 12.6       |

### Effect Tabulation

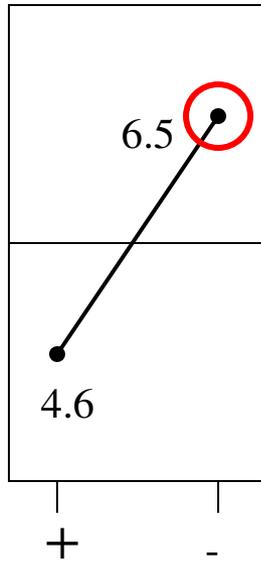
|   | A    | B    | C    | D    |
|---|------|------|------|------|
| + | 4.60 | 5.50 | 5.65 | 5.58 |
| - | 6.48 | 5.58 | 5.43 | 5.50 |



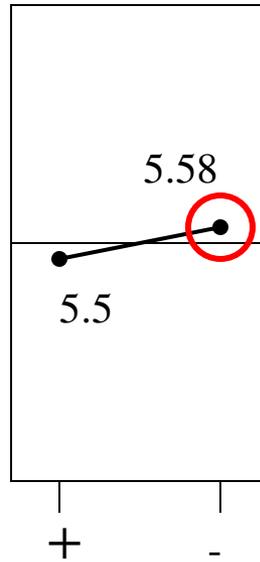
# SIX SIGMA

## Factor Effect Plot

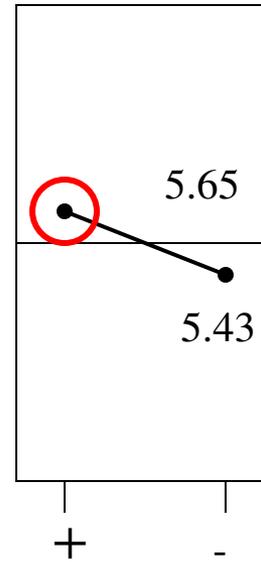
Gluing Strength ↑



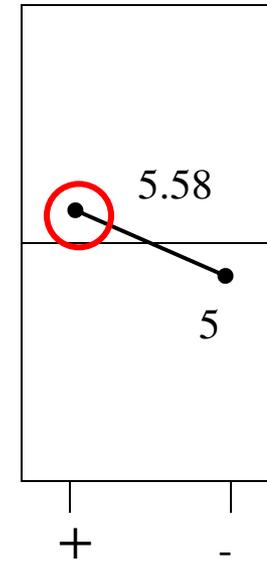
Adhesion Area



Type of Glue



Thk of Foam Styrene



Thk of logo



# SIX SIGMA

## STEPS IN PLANNING AN EXPERIMENT

1. Define Objective.
2. Select the Response (Y)
3. Select the factors (Xs)
4. Choose the factor levels
5. Select the Experimental Design
6. Run Experiment and Collect the Data
7. Analyze the data
8. Conclusions
9. Perform a confirmation run.



# SIX SIGMA

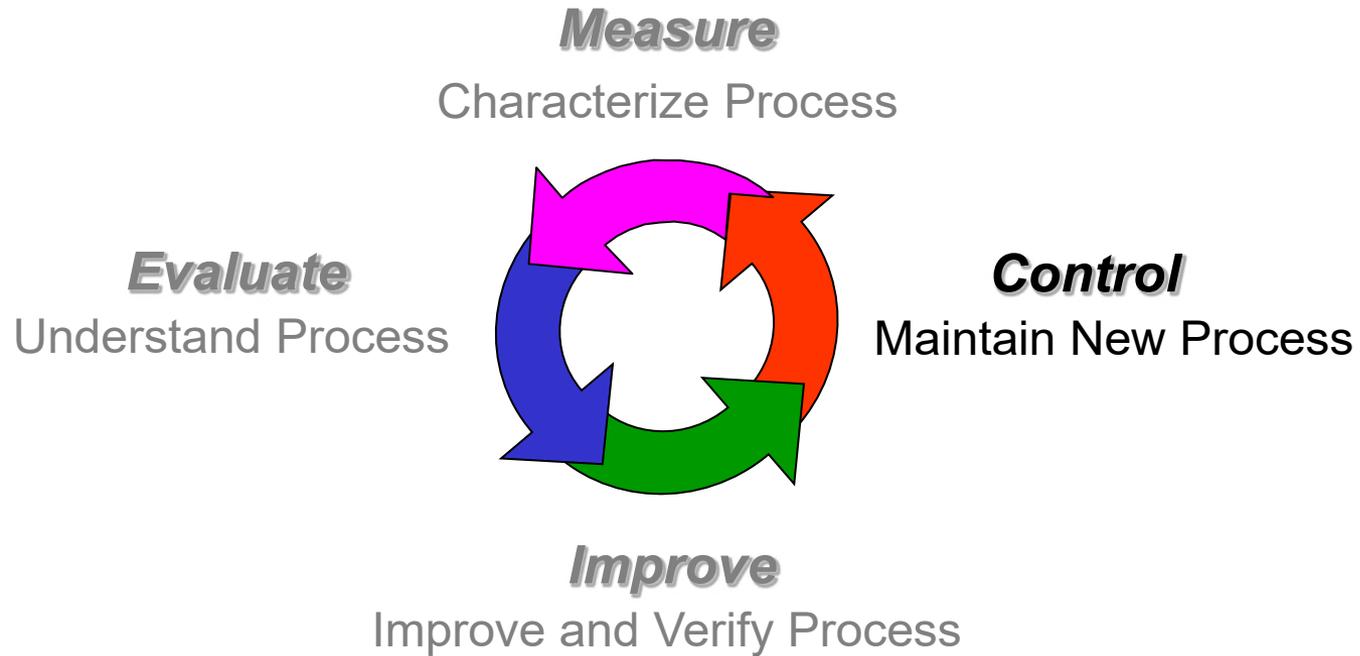
“...No amount of experimentation can prove me right; a single experiment can prove me wrong”.

“....Science can only ascertain what is, but not what should be, and outside of its domain value judgments of all kinds remain necessary.”

- Albert Einstein



# SIX SIGMA





# SIX SIGMA

## CONTROL PHASE - SIX SIGMA

### Control Phase Activities:



- Confirmation of Improvement
- Confirmation you solved the practical problem
- Benefit validation
- Buy into the Control plan
- Quality plan implementation
- Procedural changes
- System changes
- Statistical process control implementation
- “Mistake-proofing” the process
- Closure documentation
- Audit process
- Scoping next project



# SIX SIGMA

## CONTROL PHASE - SIX SIGMA

How to create a Control Plan:

1. Select Causal Variable(s). Proven vital few X(s)
2. Define Control Plan
  - 5Ws for optimal ranges of X(s)
3. Validate Control Plan
  - Observe Y
4. Implement/Document Control Plan
5. Audit Control Plan
6. Monitor Performance Metrics



# SIX SIGMA

## CONTROL PHASE - SIX SIGMA

### Control Plan Tools:

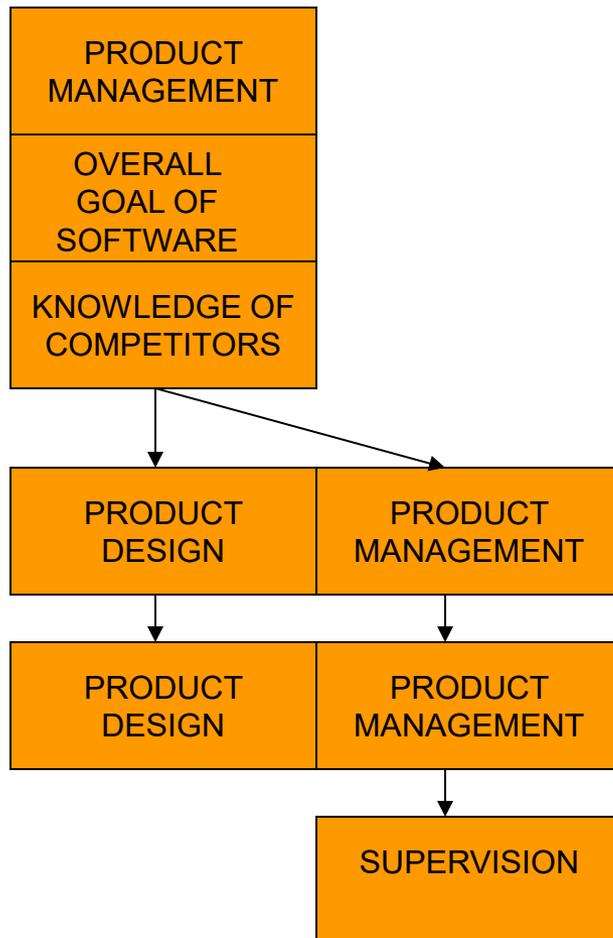
1. Basic Six Sigma control methods.
  - 7M Tools: Affinity diagram, tree diagram, process decision program charts, matrix diagrams, interrelationship diagrams, prioritization matrices, activity network diagram.
  
2. Statistical Process Control (SPC)
  - Used with various types of distributions
  - Control Charts
    - Attribute based (np, p, c, u). Variable based (X-R, X)
    - Additional Variable based tools
      - PRE-Control
      - Common Cause Chart (Exponentially Balanced Moving Average (EWMA))



# SIX SIGMA

## AFFINITY DIAGRAM

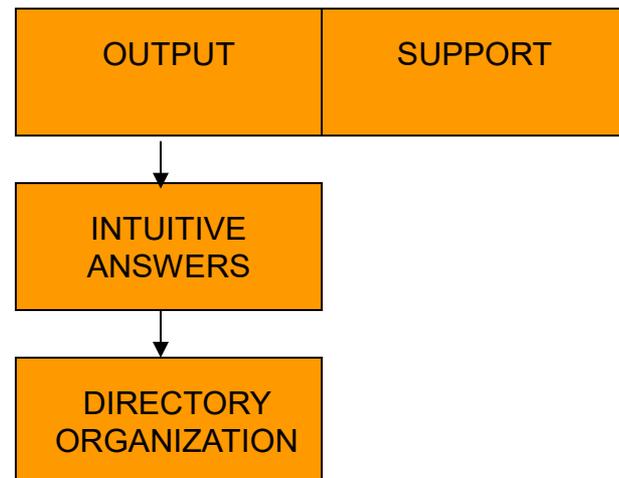
### INNOVATION



### CHARACTERISTICS:

- Organizing ideas into meaningful categories
- Data Reduction. Large numbers of qual. Inputs into major dimensions or categories.

### METHODS TO MAKE EASIER FOR USERS





# SIX SIGMA

## MATRIX DIAGRAM

HOWS

WHAT'S

RELATIONSHIP MATRIX

CUSTOMER IMPORTANCE MATRIX

|   |   | Patient scheduled | Attendant assigned | Attendant arrives | Obtains equipment | Transports patient | Provide Therapy | Notifies of return | Attendant assigned | Attendant arrives | Patient returned |
|---|---|-------------------|--------------------|-------------------|-------------------|--------------------|-----------------|--------------------|--------------------|-------------------|------------------|
| Arrive at scheduled time  | 5 | 5                 | 5                  | 5                 | 1                 | 5                  | 0               | 0                  | 0                  | 0                 | 0                |
| Arrive with proper equipment                                    | 4 | 2                 | 0                  | 0                 | 5                 | 0                  | 0               | 0                  | 0                  | 0                 | 0                |
| Dressed properly  | 4 | 0                 | 0                  | 0                 | 0                 | 0                  | 0               | 0                  | 0                  | 0                 | 0                |
| Delivered via correct mode                                      | 2 | 3                 | 0                  | 0                 | 1                 | 0                  | 0               | 0                  | 0                  | 0                 | 0                |
| Take back to room promptly                                      | 4 | 0                 | 0                  | 0                 | 0                 | 0                  | 0               | 5                  | 5                  | 5                 | 5                |
|   |   |                   |                    |                   |                   |                    |                 |                    |                    |                   |                  |
| IMPORTANCE SCORE  |   | 39                | 25                 | 25                | 27                | 25                 | 0               | 20                 | 20                 | 20                | 20               |
| RANK  |   | 1                 | 3                  | 3                 | 2                 | 3                  | 7               | 6                  | 6                  | 6                 | 6                |
| 5 = high importance, 3 = average importance, 1 = low importance |   |                   |                    |                   |                   |                    |                 |                    |                    |                   |                  |



# SIX SIGMA

## COMBINATION ID/MATRIX DIAGRAM

### CHARACTERISTICS:

- Uncover patterns in cause and effect relationships.
- Most detailed level in tree diagram. Impact on one another evaluated.

|   | Add features | Make existing product faster | Make existing product easier to use | Leave as-is and lower price | Devote resources to new products | Increase technical support budget | Out arrows | In arrows | Total arrows | Strength |
|---|--------------|------------------------------|-------------------------------------|-----------------------------|----------------------------------|-----------------------------------|------------|-----------|--------------|----------|
| ◎ (9) = Strong Influence<br>○ (3) = Some Influence<br>△ (1) = Weak/possible influence<br>↑ Means row leads to column item<br>← Means column leads to row item |              |                              |                                     |                             |                                  |                                   |            |           |              |          |
| Add features  | ■            | ↑◎                           | ↑◎                                  | ↑◎                          | ↑◎                               | ↑◎                                | 5          | 0         | 5            | 45       |
| Make existing product faster  | ←◎           | ■                            | ↑◎                                  | ↑◎                          |                                  |                                   | 2          | 1         | 3            | 27       |
| Make existing product easier to use   | ←◎           | ←◎                           | ■                                   | ○                           |                                  |                                   | 1          | 2         | 3            | 21       |
| Leave as-is and lower price   | ←◎           | ←◎                           | ←○                                  | ■                           |                                  |                                   | 0          | 3         | 3            | 21       |
| Devote resources to new products  | ←◎           |                              |                                     |                             | ■                                | ↑◎                                | 1          | 1         | 2            | 18       |
| Increase technical support budget   | ←◎           |                              |                                     |                             | ←◎                               | ■                                 | 0          | 2         | 2            | 18       |



# SIX SIGMA

## CONTROL PHASE - SIX SIGMA

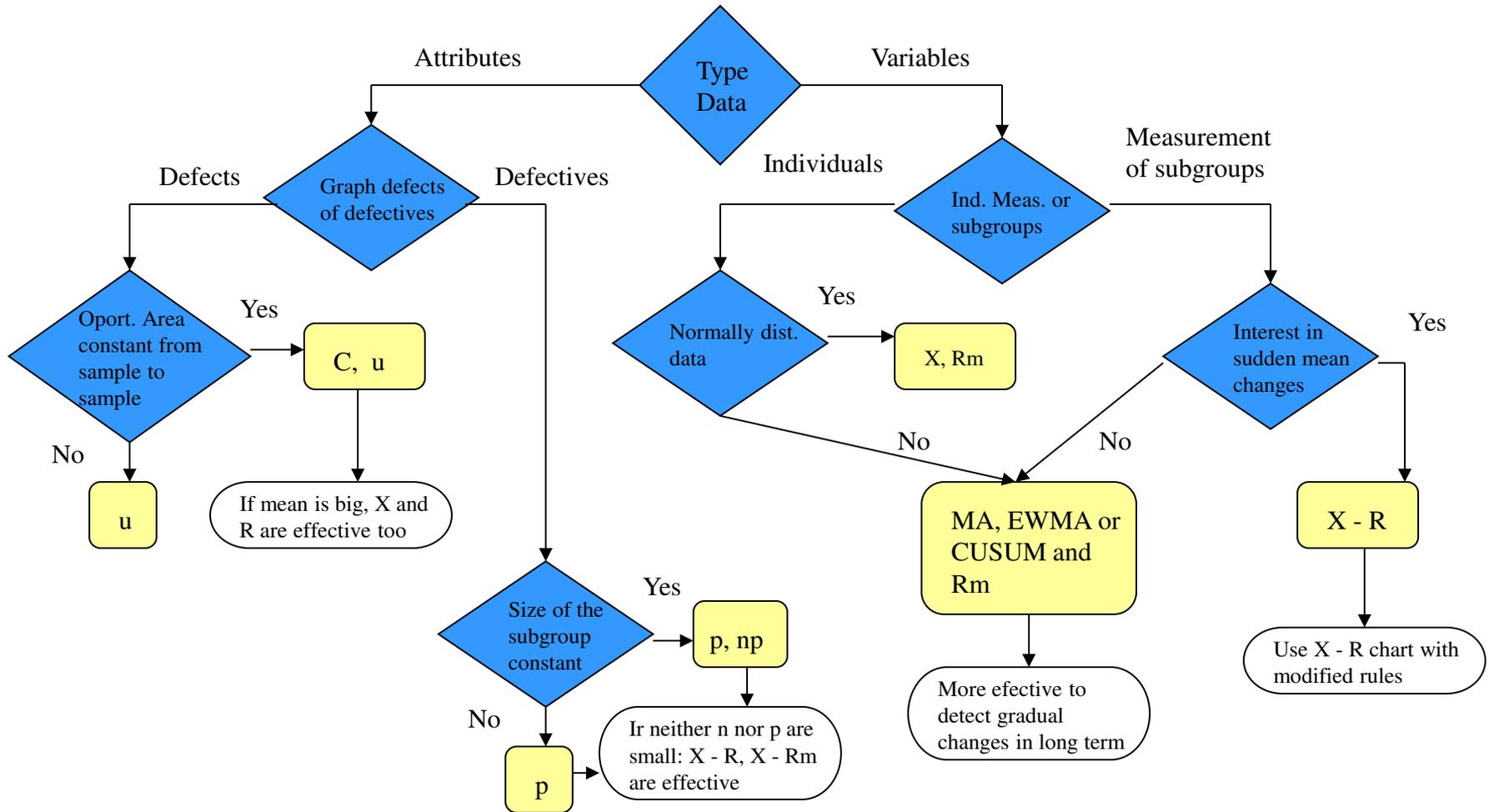
### Control Plan Tools:

1. Basic Six Sigma control methods.
  - 7M Tools: Affinity diagram, tree diagram, process decision program charts, matrix diagrams, interrelationship diagrams, prioritization matrices, activity network diagram.
  
2. Statistical Process Control (SPC)
  - Used with various types of distributions
  - Control Charts
    - Attribute based (np, p, c, u). Variable based (X-R, X)
    - Additional Variable based tools
      - PRE-Control
      - Common Cause Chart (Exponentially Balanced Moving Average (EWMA))



# SIX SIGMA

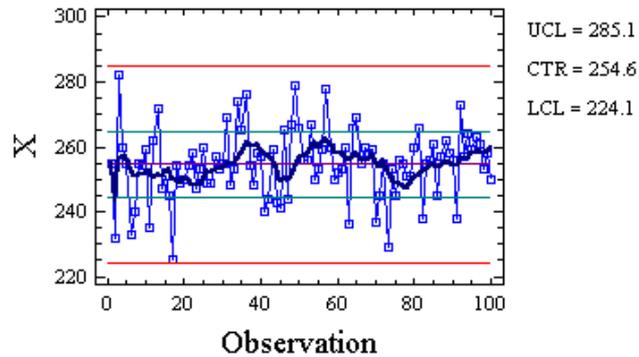
How do we select the correct Control Chart:



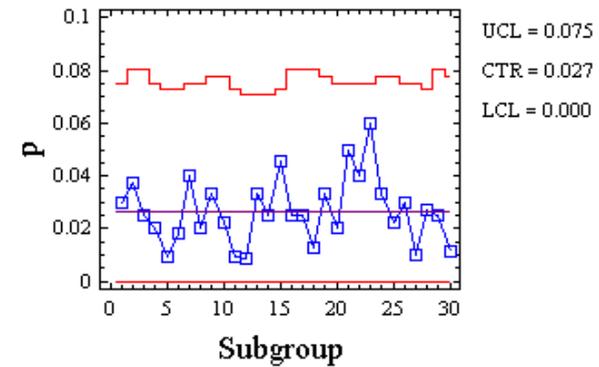


# SIX SIGMA

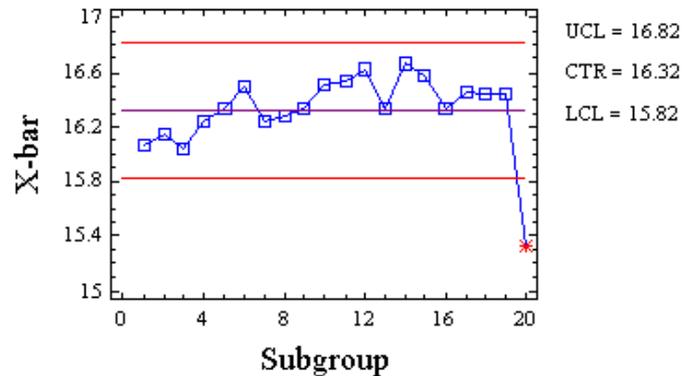
X Chart for strength



p Chart for ojdefects/ojsize



X-bar Chart for cereal



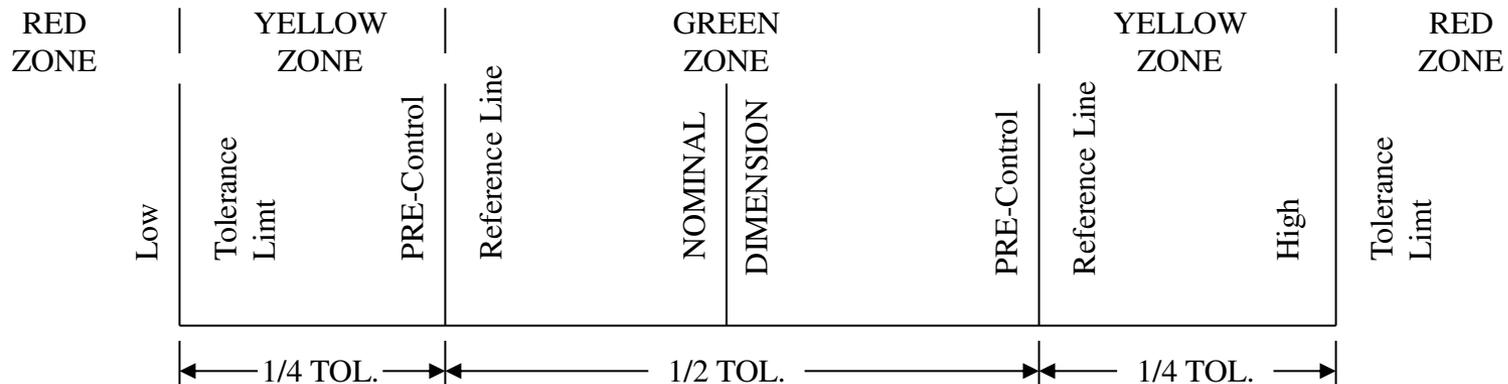


# SIX SIGMA

Additional Variable based tools:

## 1. PRE-Control

- Algorithm for control based on tolerances
- Assumes production process with measurable/adjustable quality characteristic that varies.
- Not equivalent to SPC. Process known to be capable of meeting tolerance and assures that it does so.
- SPC used always before PRE-Control is applied.
- Process qualified by taking consecutive samples of individual measurements, until 5 in a row fall in central zone, before 2 fall in cautionary. Action taken if 2 samples are in Cau. zone.
- Color coded





# SIX SIGMA

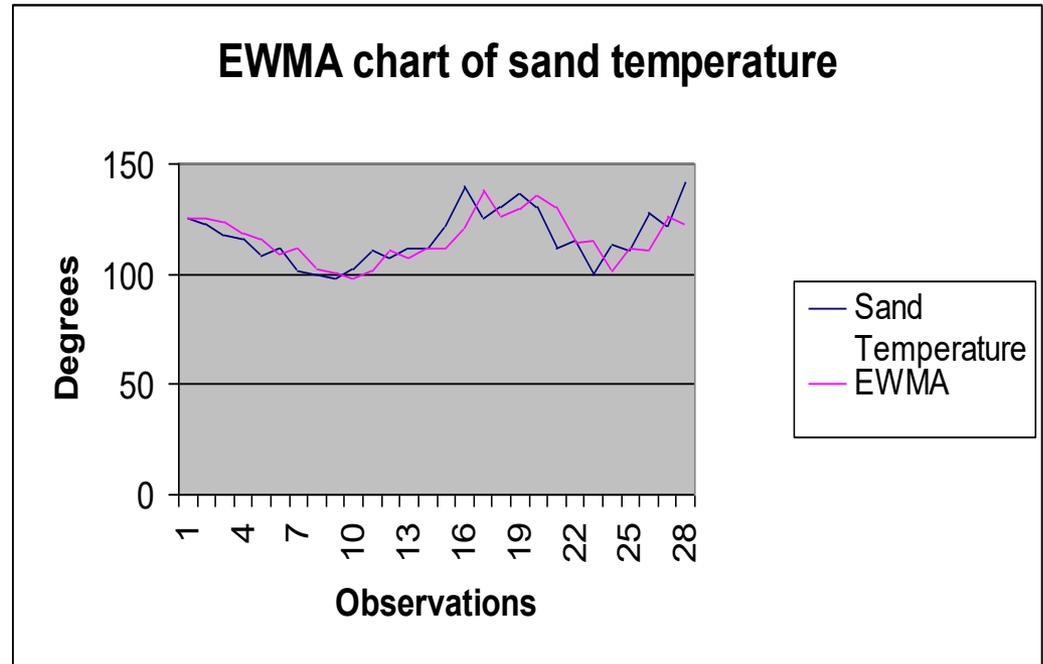
## 2. Common Causes Chart (EWMA).

- Mean of automated manufacturing processes drifts because of inherent process factor. SPC considers process static.
- Drift produced by common causes.
- Implement a “Common Cause Chart”.
- No control limits. Action limits are placed on chart.
  - Computed based on costs
  - Violating action limit does not result in search for special cause. Action taken to bring process closer to target value.
- Process mean tracked by EWMA
- Benefits:
  - Used when process has inherent drift
  - Provide forecast of where next process measurement will be.
  - Used to develop procedures for dynamic process control
- Equation:  $EWMA = y^t + \sigma (y^t - y^t)$        $\sigma$  between 0 and 1



# SIX SIGMA

| Sand Temperature | EWMA   | Error  |
|------------------|--------|--------|
| 125              | 125.00 | 0.00   |
| 123              | 125.00 | -2.00  |
| 118              | 123.20 | -5.20  |
| 116              | 118.52 | -2.52  |
| 108              | 116.25 | -8.25  |
| 112              | 108.83 | 3.17   |
| 101              | 111.68 | -10.68 |
| 100              | 102.07 | -2.07  |
| 92               | 100.21 | -8.21  |
| 102              | 98.22  | 3.78   |
| 111              | 101.62 | 9.38   |
| 107              | 110.60 | -3.60  |
| 112              | 107.30 | 4.70   |
| 112              | 111.53 | 0.47   |
| 122              | 111.95 | 10.05  |
| 140              | 121.00 | 19.00  |
| 125              | 138.00 | -13.00 |
| 130              | 126.31 | 3.69   |
| 136              | 129.63 | 6.37   |
| 130              | 135.36 | -5.36  |
| 112              | 130.54 | -18.54 |
| 115              | 113.85 | 1.15   |
| 100              | 114.89 | -14.89 |
| 113              | 101.49 | 11.51  |
| 111              | 111.85 | -0.85  |





# SIX SIGMA

## Project Closure

- Improvement fully implemented and process re-baselined.
- Quality Plan and control procedures institutionalized.
- Owners of the process: Fully trained and running the process.
- Any required documentation done.
- History binder completed. Closure cover sheet signed.
- Score card developed on characteristics improved and reporting method defined.



# SIX SIGMA

## **Motorola ROI 1987-1994**

- Reduced in-process defect levels by a factor of 200.
- Reduced manufacturing costs by \$1.4 billion.
- Increased employee production on a dollar basis by 126%.
- Increased stockholders share value fourfold.

## **AlliedSignal ROI 1992-1996**

- \$1.4 Billion cost reduction.
- 14% growth per quarter.
- 520% price/share growth.
- Reduced new product introduction time by 16%.
- 24% bill/cycle reduction.



# SIX SIGMA

## **General Electric ROI 1995-1998**

- Company wide savings of over \$1 Billion.
- Estimated annual savings to be \$6.6 Billion by the year 2000.



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